Reconstruction of the 1979–2006 Greenland ice sheet surface mass balance using the regional climate model MAR

X. Fettweis1,*

1Institut d’Astronomie et de Géophysique Georges Lemaître, Université catholique de Louvain, Louvain-la-Neuve, Belgium

*now at: Département de Géographie, Climatologie et Topoclimatologie, Université de Liège, Liège, Belgium

Received: 18 June 2007 – Published in The Cryosphere Discuss.: 3 July 2007
Revised: 25 September 2007 – Accepted: 18 October 2007 – Published: 31 October 2007

Abstract. Results from a 28-year simulation (1979–2006) over the Greenland ice sheet (GrIS) reveal an increase of solid precipitation (+0.4±2.5 km³ yr⁻¹) and runoff (+7.9±3.3 km³ yr⁻¹) of surface meltwater. The net effect of these competing factors is a significant Surface Mass Balance (SMB) loss of −7.2±5.1 km³ yr⁻². The contribution of changes in the net water vapour flux (+0.02±0.09 km³ yr⁻²) and rainfall (+0.2±0.2 km³ yr⁻²) to the SMB variability is negligible. The meltwater supply has increased because the GrIS surface has been warming up +2.4°C since 1979. Sensible heat flux, latent heat flux and net solar radiation have not varied significantly over the last three decades. However, the simulated downward infrared flux has increased by 9.3 W m⁻² since 1979. The natural climate variability (e.g. the North Atlantic Oscillation) does not explain these changes. The recent global warming, due to the greenhouse gas concentration increase induced by human activities, could be a cause of these changes. The doubling of surface meltwater flux into the ocean over the period 1979–2006 suggests that the overall ice sheet mass balance has been increasingly negative, given the likely meltwater-induced acceleration of outlet glaciers. This study suggests that increased melting overshadows over an increased accumulation in a warming scenario and that the GrIS is likely to keep losing mass in the future. An enduring GrIS melting will probably affect in the future an certain effect on the stability of the thermohaline circulation and the global sea level rise.

1 Introduction

There is almost no more doubt now that human activities are responsible for a large part of the global temperature rise observed since the beginning of the industrial era. This is mainly due to increasing greenhouse gas (GHG) emissions (Solomon et al., 2007). Consequences of a warmer climate on the Greenland Ice Sheet (GrIS) mass balance will be a thickening inland, due to increased solid precipitation, and a thinning at the GrIS periphery, due to a combination of an increasing surface melt and a probably increased iceberg discharge into the ocean along the coasts. Climatic warming increases indeed snow and ice melting over the summer but also evaporation above the ocean. This leads to higher moisture transport inland and, consequently, higher precipitation. However, increasing precipitation combined with warming suggests a simultaneous increase in summer rain occurrence, which accelerates the snow/ice melting. With higher temperatures, a large part of the precipitation will occur at low elevations under the form of rain instead of snow. The induced wetting of the snow will reduce the surface albedo; this can contribute to an abnormally early onset of melting. Meltwater run-off represents about half of the annual mass loss of the GrIS (Zwally and Giovinetto, 2001). The other main ablation processes are iceberg discharge and subglacial melting (Reeh et al., 1999). Surface water vapour fluxes are generally small in comparison with precipitation rates (Box and Steffen, 2001; Box et al., 2004). Finally, as suggested by recent observations (Rignot and Kanagaratnam, 2006), the mass lost by iceberg discharge could also increase as a consequence of global warming. Indeed, the recent acceleration of Greenland outlet glaciers (Howat et al., 2005; Luckman and Murray, 2005, 2006) could be associated to the increasing supply of meltwater reaching the glacier bed which, by lubricating the ice/bedrock interface, facilitates glacier sliding (Zwally et al., 2002). This will also lead to a thinning of the margin and cause the ice sheet to retreat from the coast as pointed out by Krabill et al. (1999). Due to the well-known albedo and elevation feedbacks, a progressive depletion of the GrIS would amplify the deglaciation (Ridley et al., 2005).

Run-off increase is expected to exceed the precipitation increase (Alley et al., 2005; Lemke et al., 2007) and,
consequently, the GrIS is likely to lose mass. In this case, the resulting freshwater increase could, on the one hand, perturb the thermohaline circulation (THC) by reducing the density contrast driving the THC (Rahmstorf et al., 2005), and on the other hand, contribute to sea level rise (Dowdeswell, 2006) under the projected global warming (Solomon et al., 2007). Recent observation-based studies show a significant surface melt increase over the GrIS (Fettweis et al., 2007; Tedesco, 2007), a thinning at the margins (Krabill et al., 1999, 2004; Thomas et al., 2006), an increased discharge from outlet glaciers (Rignot et al., 2004; Rignot and Kanagaratnam, 2006) and a growing of the ice sheet in the Greenland interior (Krabill et al., 2000; Thomas et al., 2001, 2006).

Recent GrIS observations made by laser altimeter and by NASA Gravity Recovery and Climate Experiment (GRACE) satellites rather suggest that the whole ice sheet is losing mass (Velicogna and Wahr, 2005; Chen et al., 2006; Luthcke et al., 2006; Thomas et al., 2006), although this trend is not unanimously acknowledged (Johannessen et al., 2005; Zwally et al., 2005). However, these observation-based studies are not always representative for long-term variations given the important year to year variations observed in the annual mass balance (Greuell et al., 2001; Howat et al., 2007). Therefore, large uncertainties remain in observation-based studies due to the sparse resolution of measurements in time and/or space; continued monitoring is needed to identify any significant future changes on the GrIS (Lemke et al., 2007).

Numerical models provide an unique opportunity to fill this space-time gap by determining more efficiently the whole ice sheet current mass balance evolution over longer periods (Hanna et al., 2005; Box et al., 2006). Among them, the high resolution limited-area Regional Climate Models (RCMs) nested in observation-based reanalysis offer the possibility to estimate the mass balance at spatial resolutions identical to satellite observations, by using sophisticated atmospheric physics and surface parametrizations designed for polar regions. They can be considered as being physically-based interpolators of the assimilated observations (surface weather stations, atmospheric sounding and satellite remote sensing). That is why the GrIS SMB is more and more studied with RCMs (Dethloff et al., 2002; Hanna et al., 2002; Box and Rinke, 2003; Mote, 2003; Box et al., 2006; Fettweis et al., 2006).

In order to improve predictions of the future behaviour of the GrIS in the global warming context, it is necessary to better know and assess its current state and variability. That is the reason why we have chosen in this article to simulate the GrIS SMB of the last thirty years with a coupled atmosphere-snow RCM having a horizontal resolution of 25 km. The model used is the regional climate model MAR (Modèle Atmosphérique Régional) developed by Gallée and Schayes (1994). This model has already shown its capability on the GrIS (Lefebre et al., 2003, 2005; Fettweis et al., 2005, 2006, 2007). The effective simulation starts in 1979 together with the beginning of remote sensing observations and stops at the end of 2006. Any RCM applications to the past rather than to the future benefit from the observations to drive the model (via the reanalysis) and to subsequently evaluate the model results. Furthermore, our simulation illustrates the GrIS response to the rapid warming observed in Greenland since the mid-1980’s (Chylek et al., 2006; Box and Cohen, 2006). Finally, this 28-year simulation is one of the longest simulations known by the author of the Greenland climate made with a coupled snow atmospheric RCM until now (Box et al., 2006; Fettweis et al., 2007).

After a brief description of the RCM we used in Sect. 2, Sect. 3 analyses in detail the evaluation of the SMB simulated by MAR and its interannual fluctuations over the 1979–2006 period. The MAR model shows significant changes in the 1979–2006 variability of the GrIS SMB components. The atmospheric part of the MAR model helps us to better understand these changes: Sect. 4 discusses the surface energy balance over the GrIS. Links with the North Atlantic Oscillation (NAO) are explored in Sect. 5 but the natural variability does not explain the simulated changes. The recent global warming due to increased greenhouse gas concentration could be at the origin of these changes as concluded in Sect. 6.

2 The MAR model

The model used here is the regional climate model MAR coupled to the 1-D Surface Vegetation Atmosphere Transfer scheme SISVAT (Soil Ice Snow Vegetation Atmosphere Transfer). The atmospheric part of MAR is fully described in Gallée and Schayes (1994), while the SISVAT scheme is detailed in De Ridder and Gallée (1998). The snow-ice part of SISVAT, based on the CEN (Centre d’Etudes de la Neige) snow model called CROCUS (Brun et al., 1992), is a one-dimensional multi-layered energy balance model that determines the exchanges between the sea ice, the ice sheet surface, the snow-covered tundra, and the atmosphere (Gallée et al., 2001). It consists of a thermodynamic module, a water balance module taking into account the meltwater refreezing, a turbulence module, a snow metamorphism module, a snow/ice discretization module, and an integrated surface albedo module. The blowing snow model, currently under development for the Antarctic ice sheet (Hubert Gallée, personal communication), is not yet used here. Despite changes in the wind snow erosion variability seems to be low these last years on the GrIS (Box et al., 2004, 2006), it would be very interesting in the future to test this module on the GrIS. In addition, SISVAT does not contain an ice dynamics module. We thus only present the SMB and not the Ice sheet Mass Balance (IMB) of the GrIS. Therefore, a fixed ice sheet mask to simulate the current climate is assumed.

The simulation starts in September 1977 (to reduce the impacts of the snow model initialization in 1979) and lasts till December 2006 with a spatial resolution of 25 km and
a time step of 120 s. The ERA-40 reanalysis (1977–2002) and after that, the operational analysis (2002–2006) from the European Centre for Medium-Range Weather Forecasts (ECMWF) are used to initialize the meteorological fields at the beginning of the simulation in September 1977 and to force the lateral boundaries with temperature, specific humidity and wind components during the simulation. The (re)analysis is available every 6 h at a resolution of one degree (~100 km). The Sea Surface Temperatures (SST) and the sea-ice extent in the SISVAT module are also prescribed by the reanalysis. No reinitialisations/adjustments are applied to the model outputs. The schemes and set-up used here are fully described in Fettweis et al. (2005) and Lefebre et al. (2005).

<table>
<thead>
<tr>
<th>Model</th>
<th>Period</th>
<th>Area (x10⁶ km²)</th>
<th>Snowfall</th>
<th>Rainfall</th>
<th>Subli./Dep.</th>
<th>Blowing snow</th>
<th>Accumulation</th>
<th>Run-off</th>
<th>Surface mass balance</th>
<th>Iceberg calving</th>
<th>Basal melting</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAR</td>
<td>1979–2005</td>
<td>1701</td>
<td>594±53</td>
<td>24±5</td>
<td>5±2</td>
<td>612±55</td>
<td>304±96</td>
<td>308±125</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Polar MM5</td>
<td>1988–2004</td>
<td>1691</td>
<td>617±59</td>
<td>24±7</td>
<td>64±8</td>
<td>543±131</td>
<td>373±66</td>
<td>170±152</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ECHAM4</td>
<td>1990's</td>
<td>1691</td>
<td>585</td>
<td>46</td>
<td>34±6</td>
<td>540</td>
<td>122</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MIT</td>
<td>1990's</td>
<td>1648</td>
<td>620</td>
<td>25</td>
<td>75</td>
<td>539</td>
<td>278</td>
<td>261</td>
<td>262±39</td>
<td></td>
<td></td>
</tr>
<tr>
<td>PDD model</td>
<td>1990's</td>
<td>1,691</td>
<td>649</td>
<td>95</td>
<td>554</td>
<td>542</td>
<td>281</td>
<td></td>
<td>293±104</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ECMWF analysis</td>
<td>1958–2003</td>
<td>1,684</td>
<td>620</td>
<td>25</td>
<td>75</td>
<td>539</td>
<td>278</td>
<td>261</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Reeh et al. (1999)</td>
<td>1990'</td>
<td>1,707</td>
<td>1,707</td>
<td>1,707</td>
<td>1,707</td>
<td>1,707</td>
<td>1,707</td>
<td>1,707</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3 Surface mass balance of the Greenland ice sheet

3.1 Average annual rates of the SMB components

3.1.1 Results

All the models listed in Table 1 agree unanimously to give an annual total ice sheet mass snowfall rate of ~600 km² yr⁻¹. The net erosion by surface water vapour fluxes is estimated to be ~50–100 km³ yr⁻¹ (except by the MAR model) which gives an accumulation rate (usually noted P-E) of approximately 550 km³ yr⁻¹. The MAR simulated annual snowfall and net surface water vapour fluxes are respectively plotted in Figs. 1a and 2a. The MAR solid precipitation shows spatial patterns identified in interpolation of ice core and snow pit data (e.g., Ohmura et al., 1999; Cogley, 2004) or simulated by models (e.g., Hanna et al., 2002, 2006; Box et al., 2006). See Fettweis et al. (2005) for more details about the validation of the MAR precipitation.

Unlike other models, the deposition/condensation accumulation simulated by MAR nearly dominates, in average, the sublimation/evaporation erosion over the whole ice sheet (see Table 1). Except at the summit where the small gain of mass modelled by MAR is consistent with the GC-Net observations, MAR underestimates the mass loss resulting from sublimation/deposition by comparison with the Polar MM5 outputs (Box et al., 2006) and the Box and Steffen (2001) estimates based on GC-net observations (see Fig. 2a). This problem will be investigated in the future by reviewing the turbulence scheme used in the GrIS simulations with MAR.

The run-off is estimated to be ~300 km³ yr⁻¹ (except by the ECHAM4 and MIT models), which gives an estimation of the SMB around 300 km³ yr⁻¹ when balancing the glacier discharge and basal melting rate as estimated by Reeh et al. (1999). Their glacier discharge estimation represents a minimum value under current climatic conditions according to Box et al. (2006) because they do not account for the melt-induced outlet glacier acceleration observed by Zwally et al. (2002). The larger run-off rate simulated by the Polar MM5 model could be partly explained by the discrepancies in the used ice sheet mask i.e. in the classification of ice/land/ocean land surface type. Along the southeastern coast, the MM5 ice sheet margin runs directly along the coastline, which increases significantly the melt overall. Other ice sheet masks (Mote, 2003; Fettweis et al., 2005; Hanna et al., 2005) define tundra grid points between the ice sheet margin (which lies at higher altitude as a result) and the sea. Besides, the MM5 SMB estimation is the only model taking into account snow erosion by the wind. The ECHAM4 and MIT models...
Fig. 1. The 1979–2006 annual mean (left), 28-year linear regression change (centre) and autocorrelation (right) of the snowfall. Units are mm of water equivalent (mmWE) The autocorrelation is defined as the correlation between time series of the annual total ice sheet snowfall with that at each grid location. The autocorrelation shows where regional variability best captures the variability over the complete ice sheet. Under each plot, minimum and maximum values are indicated as well as the ice sheet average and the standard deviation.

Fig. 2. Same as Fig. 1 but for the net surface water vapour fluxes (i.e. the evaporation, condensation, sublimation and deposition).

underestimate the ablation rate due to the absence of run-off along the northern coast of the ice sheet according to Bugnion and Stone (2002).

While the MAR model underestimates the sublimation/evaporation mass loss, it is consistent with other models by giving a SMB rate of 308 km$^3$ yr$^{-1}$. In addition, the
MAR patterns shown in Fig. 3a fully agree with other estimations based on both observations (Zwally and Giovinetto, 2001) and models (Box et al., 2004, 2006; Hanna et al., 2005) The MAR sublimation/evaporation underestimation can be assumed to be systematic each year. Therefore, it is reasonable to suppose that it weakly affects the temporal variability of the components simulation and that the MAR results can be used in a reliable way to study the SMB components evolution over the last 28 years. However, the accuracy of our model needs to be improved in the future to produce more reliable assessments of surface mass budget terms and their temporal changes.

3.1.2 Discussion

Contrary to Box et al. (2006) and Hanna et al. (2007) who calibrated SMB outputs during or after the simulation, the MAR outputs are not recalibrated and corrected. However, the use of remote sensing observations (as melt estimate from Tedesco, 2007) during the MAR simulation could improve our modelled SMB results. For example, remote data (albedo, liquid water content) easily detects the presence of bare ice/fresh snow in the ablation zone in summer. In the case of discrepancies between MAR and remote data, the MAR snow pack could be updated tracking down the precise time, when bare ice appears in the ablation zone in summer, has a great impact on the simulated SMB because of the albedo feedback (Lefebre et al., 2005). Applying these changes during the simulation (instead of after) allows the model to take directly into account the feedback mechanisms of the bare ice apparition.

In addition, the modelled run-off could be validated with satellite derived observations (the run-off rate could be derived from changes in the snow pack liquid water content). The run-off rate differs for each model listed in Table 1. It constitutes the largest uncertainty in the current SMB estimations because no observations are available to validate this flux on which predicted sea level rise and THC perturbations depend. In the global warming context, this meltwater flux could change quickly and a good knowledge of its current behaviour is needed to make accurate projections in the future.

Finally, the model results for the GrIS SMB components (especially the run-off) vary quite a lot from one another. It is clear that some of the disagreements between the models come from biases within the models as well as from large differences in the processes resolved by the snow model and the coupling with the atmosphere: i) The MAR climate model has a complex snow model fully coupled with the atmospheric module running at the same resolution (i.e. 25 km); ii) The MM5 model used by Box et al. (2006) is an atmospheric weather model running at a resolution of 24 km and it is coupled with a simplified snow model which takes however into account the blowing snow erosion (Snow pack properties in MM5 mainly derive from the direct measurements driving the model during simulation); iii) The Hanna et al. (2007) estimations use a complex snow model running...
Fig. 4. Time series of the annual total ice sheet (a) SMB, (b) snowfall, (c) run-off, (d) net water vapour fluxes, (e) SMB averaged over the ice sheet area below 2000 m and (f) above 2000 m. The correlation with the whole ice sheet SMB is indicated as well as the trend. The linear trends are in km$^3$ yr$^{-2}$.

at a resolution of 5 km forced by monthly mean atmospheric fields from the ECMWF (re)analysis available at a resolution of 110 km; iv) The Mote (2003) estimations use a Positive Degree Day (PDD) model at a resolution of 25 km forced by the SSM/I brightness temperature and by the Bromwich et al. (2001) accumulation time series. But, the used ice sheet mask, the resolution and the spin-up time could also be a cause of disagreement between models. Their impacts on the modelled SMB results should be investigated in the future:

- First, a too large ice sheet mask (i.e. with low-altitude pixels, where there is no ice) leads to an overestimation of the run-off (as discussed in Sect. 3.1.1 for the MM5 results). A model with a too small ice sheet area will rather overestimate the SMB. In addition, due to the albedo feedback, biases in the ice sheet mask will also have an impact on the surface energy balance.

- Secondly, the resolution (and then the topography) used in a model can significantly influence the simulated SMB because the ablation zone where substantial
seasonal melting occurs, is not wider than 100 km in Greenland. A too coarse resolution the model from resolving adequately the steep ice sheet margin and the ablation zone. The resolution impacts also the precipitation (Fettweis et al., 2005).

- Thirdly, modelling results are very sensitive to the spin-up time used in the snow model. At the beginning of the summer, the ice sheet and the tundra are covered by the winter snow accumulation. Either climatologic precipitation data or reanalysis are used to initialize the snow model at the end of the spring, or the winter accumulation is simulated by the model itself by beginning the simulation at the end of the previous summer. Previous MAR simulations showed a very large sensitivity to the initial snow height and the snow properties above the tundra and the ablation zone given the albedo feedback (Lefebre et al., 2005). A too thick snow pack at the beginning of the summer above the ablation zone delays the appearance of bare ice (with a lower albedo) in the ablation zone and can considerably reduce the melting. That is why it is preferable to begin the simulation at the end of the previous summer (or several years before) in order to reduce the problem of the snow model initialization. For example, let us quote the MAR model which uses a spin-up of 2–3 years while the surface in MM5 model is reinitialized every day with a spin-up time of 6 hours due to the fact that MM5 is used in a forecast mode (Box et al., 2006). To reduce the impacts of the reinitialization, MM5 is however driven by data (SMB measurements from the GC-Net Automatic Weather Stations and remote sensing derived surface albedo) independent of the ECMWF atmospheric analyses used to force the model at its boundaries.

3.2 Temporal variability and trend of the SMB components

The SMB is governed, on the one hand by accumulation (snowfall) and on the other hand, by run-off (temperature). The interannual variability in precipitation and ablation causes SMB fluctuations with a correlation of respectively 0.71 and −0.90, see Fig. 4. In 1985, the SMB rate is abnormally low mainly because of low snowfall (see Table 2). Other SMB minima, rather due to a high freshwater flux into the ocean, are found in 1998 and 2003 in agreement with the Hanna et al. (2007) estimations. The absolute minimum of the SMB is reached in 2006 due to high run-off and very low snowfall. Maxima of SMB occur in two cases: in 1983 and 1992 after the volcanic eruptions from El Chichon and Mount Pinatubo that induced cooling and low melting rates; in 1996, owing to both negative run-off and positive snowfall anomalies, the SMB reaches a positive record rate as in Hanna et al. (2007). Integrated over the ice sheet, the 28-year snowfall rate shows a positive trend of +0.4 ± 2.5 km$^3$ yr$^{-2}$. The uncertainty range of the snowfall trend (denoting two standard deviations of the trend i.e. a significance of 95%) indicates clearly that the trend is not significant according to Appendix A. The run-off increase is evaluated to be +7.9 ± 3.3 km$^3$ yr$^{-2}$ (with a significance of 98%) which gives a global average sea level rise of (+2.2 ± 0.9) × 10$^{-2}$ mm yr$^{-2}$. The computation was made by using an area of a world ocean area of 361 million km$^2$. As only the run-off increase is significant against the snowfall increase, the net effect of these competing factors is a 95%-significant SMB mass loss rate, simulated to be −7.2 km$^3$ yr$^{-2}$ with an uncertainty range of ±5.1 km$^3$ yr$^{-2}$. The contribution of changes in net water vapour fluxes to the SMB variability is negligible (+0.02 ± 0.1 km$^3$ yr$^{-2}$), in

<table>
<thead>
<tr>
<th>Year</th>
<th>Snowfall</th>
<th>Rainfall</th>
<th>Subl./Evap.</th>
<th>Runoff</th>
<th>SMB</th>
<th>Temp. Ano.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1979</td>
<td>592.2</td>
<td>18.7</td>
<td>3.0</td>
<td>202.7</td>
<td>405.2</td>
<td>−0.3</td>
</tr>
<tr>
<td>1980</td>
<td>592.8</td>
<td>17.8</td>
<td>7.1</td>
<td>276.4</td>
<td>327.1</td>
<td>0.4</td>
</tr>
<tr>
<td>1981</td>
<td>572.6</td>
<td>27.6</td>
<td>6.2</td>
<td>281.7</td>
<td>312.3</td>
<td>−0.8</td>
</tr>
<tr>
<td>1982</td>
<td>532.6</td>
<td>17.0</td>
<td>6.1</td>
<td>255.1</td>
<td>288.4</td>
<td>−1.0</td>
</tr>
<tr>
<td>1983</td>
<td>638.3</td>
<td>24.5</td>
<td>2.8</td>
<td>131.7</td>
<td>528.3</td>
<td>−2.2</td>
</tr>
<tr>
<td>1984</td>
<td>648.0</td>
<td>27.7</td>
<td>3.4</td>
<td>226.1</td>
<td>446.1</td>
<td>−1.2</td>
</tr>
<tr>
<td>1985</td>
<td>490.3</td>
<td>19.1</td>
<td>9.1</td>
<td>335.6</td>
<td>164.7</td>
<td>0.6</td>
</tr>
<tr>
<td>1986</td>
<td>612.0</td>
<td>18.7</td>
<td>5.7</td>
<td>200.3</td>
<td>424.8</td>
<td>−0.5</td>
</tr>
<tr>
<td>1987</td>
<td>577.9</td>
<td>18.9</td>
<td>3.2</td>
<td>311.9</td>
<td>281.8</td>
<td>0.4</td>
</tr>
<tr>
<td>1988</td>
<td>564.5</td>
<td>23.8</td>
<td>6.6</td>
<td>277.4</td>
<td>304.3</td>
<td>−0.1</td>
</tr>
<tr>
<td>1989</td>
<td>532.6</td>
<td>27.8</td>
<td>6.2</td>
<td>300.9</td>
<td>253.4</td>
<td>−1.4</td>
</tr>
<tr>
<td>1990</td>
<td>589.1</td>
<td>25.3</td>
<td>6.7</td>
<td>316.5</td>
<td>291.2</td>
<td>−0.7</td>
</tr>
<tr>
<td>1991</td>
<td>618.8</td>
<td>22.5</td>
<td>4.2</td>
<td>311.6</td>
<td>325.5</td>
<td>−0.5</td>
</tr>
<tr>
<td>1992</td>
<td>640.7</td>
<td>14.9</td>
<td>1.5</td>
<td>99.3</td>
<td>554.7</td>
<td>−1.9</td>
</tr>
<tr>
<td>1993</td>
<td>584.6</td>
<td>24.0</td>
<td>5.9</td>
<td>264.6</td>
<td>338.1</td>
<td>−1.3</td>
</tr>
<tr>
<td>1994</td>
<td>571.5</td>
<td>21.7</td>
<td>6.1</td>
<td>229.6</td>
<td>357.6</td>
<td>−0.8</td>
</tr>
<tr>
<td>1995</td>
<td>582.3</td>
<td>22.1</td>
<td>6.0</td>
<td>317.9</td>
<td>280.6</td>
<td>0.3</td>
</tr>
<tr>
<td>1996</td>
<td>730.0</td>
<td>24.9</td>
<td>3.1</td>
<td>194.3</td>
<td>557.6</td>
<td>1.1</td>
</tr>
<tr>
<td>1997</td>
<td>662.7</td>
<td>24.2</td>
<td>5.0</td>
<td>295.1</td>
<td>386.9</td>
<td>0.7</td>
</tr>
<tr>
<td>1998</td>
<td>560.7</td>
<td>24.8</td>
<td>6.5</td>
<td>427.3</td>
<td>151.7</td>
<td>1.3</td>
</tr>
<tr>
<td>1999</td>
<td>638.6</td>
<td>24.6</td>
<td>1.5</td>
<td>320.3</td>
<td>341.4</td>
<td>0.0</td>
</tr>
<tr>
<td>2000</td>
<td>617.9</td>
<td>37.6</td>
<td>2.6</td>
<td>364.6</td>
<td>288.2</td>
<td>0.6</td>
</tr>
<tr>
<td>2001</td>
<td>660.4</td>
<td>23.8</td>
<td>3.8</td>
<td>372.1</td>
<td>308.2</td>
<td>1.2</td>
</tr>
<tr>
<td>2002</td>
<td>552.0</td>
<td>27.0</td>
<td>9.0</td>
<td>410.9</td>
<td>159.1</td>
<td>1.3</td>
</tr>
<tr>
<td>2003</td>
<td>601.7</td>
<td>33.4</td>
<td>7.5</td>
<td>526.9</td>
<td>100.7</td>
<td>1.3</td>
</tr>
<tr>
<td>2004</td>
<td>579.4</td>
<td>23.8</td>
<td>5.3</td>
<td>442.9</td>
<td>151.7</td>
<td>0.9</td>
</tr>
<tr>
<td>2005</td>
<td>607.1</td>
<td>21.5</td>
<td>7.5</td>
<td>408.3</td>
<td>212.8</td>
<td>1.6</td>
</tr>
<tr>
<td>2006</td>
<td>472.7</td>
<td>26.1</td>
<td>4.7</td>
<td>409.7</td>
<td>84.4</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Mean 593.7 23.9 5.2 304.0 308.4 0.0
Min 472.7 14.9 1.5 99.3 84.4 −2.2
Max 730.0 37.6 9.1 526.9 557.6 1.6
Range 53.4 4.9 2.1 96.2 125.0 1.1
Trend 0.4 0.3 0.0 7.9 −7.2 0.1
Fig. 5. Rates of elevation change (dS/dt) in cm yr$^{-1}$ for the 1992–2003 and the 1979–2006 periods. Only the changes due to the interannual variability of the snowfall, melt and water vapour fluxes are taken into account here. The topography (and consequently the margin glaciers) of the ice sheet is assumed to be constant during the simulation.

Table 3. Rates of surface elevation change (dS/dt) simulated by the MAR model, derived from ERS satellite radar altimeter data (Johannessen et al., 2005; Zwally et al., 2005), the NASA’s airborne (Airborne Topographic Mapper, ATM), and the satellite (ICEsat) laser altimeter surveys (Thomas et al., 2006). The period over which it is averaged is shown. Units are mm yr$^{-1}$.

<table>
<thead>
<tr>
<th>Data</th>
<th>Period</th>
<th>&lt;1500 m</th>
<th>≥1500 m</th>
<th>&lt;2000 m</th>
<th>≥2000 m</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAR model</td>
<td>1979–2006</td>
<td>−29±16</td>
<td>−15±27</td>
<td>−40±24</td>
<td>−4±20</td>
<td>−9±8</td>
</tr>
<tr>
<td>MAR model</td>
<td>1992–2003</td>
<td>−103±80</td>
<td>−44±120</td>
<td>−137±99</td>
<td>−10±83</td>
<td>−29±34</td>
</tr>
<tr>
<td>ERS data (Johannessen et al., 2005)</td>
<td>1992–2003</td>
<td>−20±9</td>
<td>+64±5</td>
<td>+25±7</td>
<td>+65±4</td>
<td>+54±2</td>
</tr>
<tr>
<td>ERS data (Zwally et al., 2005)</td>
<td>1992–2002</td>
<td>−56±14</td>
<td>+42±5</td>
<td>−14±12</td>
<td>+48±2</td>
<td>+27±3</td>
</tr>
<tr>
<td>ATM/ICEsat data (Thomas et al., 2006)</td>
<td>1993–2004</td>
<td>−257±30</td>
<td>+12±10</td>
<td>−153±17</td>
<td>+24±10</td>
<td>−45±11</td>
</tr>
</tbody>
</table>

agreement with Box et al. (2006). As shown in Fig. 4e and f, the heavier precipitation in the accumulation zone partly offsets the significant melt increase in the ablation zone. Indeed, the SMB variability shows an insignificant positive trend above 2000 m (+0.7±1.7 km$^3$ yr$^{-2}$) against a significant negative trend of −7.8±4.0 km$^3$ yr$^{-2}$ below 2000 m.

Over the 1979–2006 (resp. 1992–2003) period, MAR simulates a GrIS mean surface elevation decrease of −9±8 mm yr$^{-1}$ (resp. −29±34 mm yr$^{-1}$). Only the elevation change over 1979–2006 is 95%-significant according to Appendix A. Patterns are shown in Fig. 5 and changes simulated by MAR below/above 1500 m/2000 m are summarized in Table 3. Only the decreases below 1500/2000 m are significant. These results are fully consistent with recent observations of surface elevation changes from satellite and aircraft altimeter shown in Table 3 (Johannessen et al., 2005; Zwally et al., 2005; Thomas et al., 2006). Highest consistency is found with the last available observations derived estimations from Thomas et al. (2006) showing also a GrIS surface elevation decrease over the 1993–2004 period. Previous ERS satellite radar altimeter estimates showing rather a GrIS elevation increase are not consistent with other studies (e.g. Velicogna and Wahr, 2005; Chen et al., 2006; Luthcke et al., 2006) and need therefore to be considered with caution as discussed by Thomas et al. (2006). In addition, the interannual variability is very important and a 12-year long data set is still too short to establish long-term trends.

The melt increase occurs everywhere along the ice sheet margin (Fig. 6b) according to the GrIS warming shown in Fig. 7a. Warming is more pronounced above the ice sheet
Fig. 6. Same as Fig. 1 but for the available meltwater. Part of this meltwater is refrozen and does not reach the ocean (Lefebre et al., 2003).

Fig. 7. The 28-year linear regression change for the summer 3m-Temperature (left), for the summer downward infrared radiation (centre) and for the summer solar net radiation (right).

than along its margin, given that the surface temperature of melting snow/ice is limited to 0°C. The higher positive snowfall trend occurs near the south-eastern snowfall maximum (Fig. 1b) and negative trends are found along the ice sheet margin (lower in altitude). These negative trends are partly explained by the warming, which causes an increase in the amount of liquid precipitations versus solid ones (Fig. 8b). These changes increase the meltwater supply and also impact glacier flow lubrication according to Zwally et al. (2002). Finally, Fig. 1c shows that the snowfall at Summit is an
Fig. 8. Same as Fig. 1 but for rainfall.

Fig. 9. Time series of the total ice sheet (a) summer (from 1 May to 30 September) temperature average (in °C su-1) and (b) yearly rainfall (in km$^3$ yr$^{-1}$). The correlation with the run-off (Fig. 4) is indicated as well as the trend.

excellent indicator of the total ice sheet snowfall variability; this fully justifies the choice of this location for ice-core Greenland climate reconstructions. Given that the melt increases everywhere, positive trends in the SMB occur only in the extreme South of the GrIS where snowfall increases and dominates over ablation (Fig. 3b). MAR simulates negative 28-year SMB trends almost everywhere in the ablation zone (in red in Fig. 3a) and a significant positive SMB trend in the south-eastern of the GrIS. Figure 3c fully justifies SMB measurements near the K-Transect (in the south-western ablation zone) as records of the total GrIS SMB variability (Greuell et al., 2001).

The summer temperature exhibits a robust correlation with the meltwater supply and therefore with the run-off (0.86) from the ice sheet as a whole (Fig. 9). This provides the basis for degree-day models. The occurrence of heavier rainfalls also increases the liquid water supply. It is a fact that the liquid fraction of the overall precipitation is increasing on the GrIS (+0.2±0.2 km$^3$ yr$^{-2}$) but it does not explain more than 5% of the positive run-off 28-year trend estimated by
Fig. 10. Average equilibrium line altitude variations in MAR simulation (solid) and estimated by Zwally and Giovinetto (2001) parametrization (dashed). The MAR 28-year changes are also shown (dotted).

Fig. 11. Time series of the winter (from 1 October YEAR-1 to 30 April YEAR) snowfall before the considered year (in km$^3$ yr$^{-1}$) over (a) the ice sheet and (b) the tundra. The correlation with the SMB (Fig. 4) is indicated.

MAR (+7.9±3.2 km$^3$ yr$^{-2}$). The large part of the run-off acceleration is explained by the warming, estimated by MAR to be 0.09±0.04°C yr$^{-1}$. According to (Box et al., 2004), these considerations allow us to estimate the SMB anomaly for the entire ice sheet from the annual (yr) and June-July-August (JJA) temperature and the snowfall anomalies despite that these are not correlated. We have then:

$$\Delta SMB_{\text{GrIS}} = -64.77 \Delta T_{\text{GrIS}}^\text{yr} + 1.57 \Delta SF_{\text{GrIS}}^\text{yr}$$  \hspace{1cm} (1)

$$\Delta SMB_{\text{GrIS}} = -69.36 \Delta T_{\text{GrIS}}^\text{JJA} + 1.19 \Delta SF_{\text{GrIS}}^\text{yr}$$  \hspace{1cm} (2)

where $\Delta SMB_{\text{GrIS}}$ is the annual GrIS SMB anomaly in km$^3$, $\Delta T_{\text{GrIS}}$ is the annual (resp. JJA) GrIS 3m-temperature anomaly in K and $\Delta SF_{\text{GrIS}}$ is the annual GrIS snowfall anomaly in km$^3$. The correlation ($r$) and the root mean square error (RMSE) between the SMB simulated anomaly and the SMB estimated anomaly are $r=0.91$ and RMSE=50.3 km$^3$ (resp. $r=0.96$ and RMSE=34.33 km$^3$). Such correlations confirm our hypothesis about the acute sensitivity to the SMB to both temperature and snowfall anomalies. If we use only the JJA temperature (in K) and the annual snowfall anomalies (in mmWE) taken at Summit (the pixel used here has a latitude of 72.52° N, a longitude of 38.50° W and an altitude of 3232 m) to estimate the annual GrIS SMB anomaly
3.3 The Equilibrium Line Altitude

The Equilibrium Line Altitude (ELA) is defined as the elevation where the SMB equals zero. Therefore, the ELA provides an useful indicator of the combined influence of thermal and precipitation forcing on the SMB. Our results (see Fig. 10) are consistent with Zwally and Giovinetto (2001) parametrisation. The general pattern is obviously a lowering of the ELA with increasing latitude. Regional variation in the ELA versus latitude pattern results from changes in local topography and precipitation regimes due to the proximity or not of dominant cyclonic systems. The relatively weak ELA at 61° N across the GrIC results, for example, from abundant snowfall observed in this region (see Fig. 1a). The
trends for these last 28 years is a positive shift of +4.9 m yr$^{-1}$ (resp. +12.6 m yr$^{-1}$) of the western (resp. eastern) Greenland ELA. The positive shift of the ELA occurs everywhere (in red in Fig. 10) except at 62º N in western Greenland which is the only region where the SMB is increasing (see Fig. 3b). These results corroborate the dominance of the thermal factors variability on the SMB.

3.4 The albedo-temperature feedback

Mote (2003) suggests that high accumulation years are often associated with low ablation for the entire ice sheet due to the well-known albedo-temperature feedback. Low accumulation rates lead to more rapid losses of winter snow and to higher degree day factors for bare ice in the ablation zone. The thicker the snow pack at the end of spring, the later the bare ice (with a lower albedo) appears (Fettweis et al., 2005). A good example of the hypothesis of Mote (2003) is 1996 (see Table 2) but Fig. 11 reveals however that this hypothesis does not explain the SMB variations of these last 28 years. Indeed, the winter snow accumulation has not significantly changed while the SMB variability suggests a negative trend. As already explained, we have found that the thermal factors dominate currently the SMB sensitivity rather than the precipitation changes. These last results confirm our assumption.

4 Surface energy balance of the Greenland ice sheet

Since 1979, the SMB has been decreasing due to increasing run-off rates explained by higher temperatures. Only the increase of the long wave downward (LWD) flux and the decrease of surface albedo can explain this warming as shown in Fig. 12. No significant change occurs in both sensible and latent heat fluxes since 1979. The short wave downward (SWD) flux interannual fluctuations are very weak during the last 28 years except the negative anomalies in 1983 and 1992 due to the eruption of El Chichón and Mount Pinatubo, respectively (Hanna et al., 2005). These volcanic eruptions injected large amounts of aerosols in the atmosphere; this reduced the amount of solar energy reaching the Earth surface. Therefore, the net solar radiation (SWDn=SWD×(1−α)) has been increasing due to a decrease of the surface albedo (α). Increased melting undoubtedly reduces the surface albedo, which then obviously amplifies the warming-related melt increase. This amplification is particularly visible in the North-East Greenland tundra where the snow cover has been disappearing earlier in the summer these last years (see Fig. 7). In the previous section, we have shown that the winter accumulation variability can not explain the albedo variability; Fig. 13 confirms that the albedo decrease over the 1979–2006 period starts after the middle of the summer in the tundra due to higher temperatures. Therefore, it seems reasonable to conclude that SWDn changes are primarily driven by

![Fig. 13. Time series of the average tundra albedo for April, May, June, July and August. The 1979–2006 linear trend is dotted.](image-url)

the melt increase and, to a lesser extent, by the rainfall increase which humidifies the snow pack and reduces the surface albedo (Fig. 8). Consequently, only the positive LWD tendency leads to the overall warming of the ice sheet surface. The net solar radiation increase is besides restricted to the ablation zone and the tundra while the infrared radiation, as well as the 3m-temperature, have been increasing everywhere. The temperature is obviously better correlated with the infrared radiation than with the solar net radiation as can be seen in Fig. 14.

5 The North Atlantic Oscillation

The North Atlantic Oscillation (NAO) represents the dominant mode of regional atmospheric variability around Greenland (e.g. Rogers, 1997; Appenzeller et al., 1998; Bromwich et al., 1999) and is gauged here by the NAO index, which is computed as the normalised pressure difference between Gibraltar minus Reykjavik (Jones et al., 1997; Osborn, 2004). It is closely related to the Arctic Oscillation (AO) (Thompson et al., 1998) and is one of the major modes of variability of the Northern Hemisphere atmosphere, particularly in winter. Moreover, a large fraction of the climate changes observed during the last decades in the Arctic could be related to the positive trend in the NAO/AO index during this period (e.g., Rigor et al., 2000; Moritz et al., 2003; Hanna and Cappelen, 2003; Rogers et al., 2004; Johannessen et al., 2005). The NAO is characterized by a dipole of surface pressure between mid- and high-latitudes, resulting in changes in the strength of the westerly winds at mid-latitudes.
Fig. 14. Correlation coefficient in the summer between the 3m-temperature and the infrared radiation (left) and the net solar radiation (right), respectively. The correlation coefficient is computed by using the annual time series of each pixel.

Fig. 15. Seasonal temperature sensitivity of the Greenland ice sheet to the NAO. Only correlation coefficients above 0.3 are significant. The maps represent from left to right: the annual, winter (DJF), spring (MAM), summer (JJA) and autumn (SON) mean. The source of the NAO index comes from the Climate Research Unit (CRU), at http://www.cru.uea.ac.uk/cru/data/nao.htm.

and large winter temperature variations. A positive NAO phase shows a stronger than usual subtropical high pressure centre and a deeper than normal Icelandic low. The increased pressure difference results in more numerous and stronger winter storms crossing the Atlantic Ocean on a more northerly track. This results in warm and wet winters in
According to recent observations from Johannessen et al. (2005), the maximum of the GrIS sensitivity to the NAO variability is found in winter (DJF) (Table 4). The temperature (via the long wave radiations) is the most sensitive component and is significantly anti-correlated to the NAO as already pointed out by Chylek et al. (2004). When the NAO index is negative, the location of the Icelandic low favours (southerly) warm air advection along the southwest coast of Greenland and over the ice sheet. This explains why the temperature correlation with the NAO is maximum in the south(west) of Greenland (Fig. 15). Everywhere and during every season, the temperature is anti-correlated to the NAO although this correlation is not significant in summer (JJA), in particular along the northeastern coast as found by Chylek and Lohmann (2005).

Modelled precipitation variability also presents significant links with the NAO (Fig. 16). Consistent with the regional temperature sensitivity, a positive NAO phase (i.e. cold winter) is associated with less precipitation in the southeast in winter (DJF) and autumn (SON). Generally, when the NAO is positive, stronger westerlies reduce the southwesterly flow that brings moisture to Greenland, resulting in an average reduction of the snow accumulation. On the contrary, when the NAO is negative, the large-scale atmospheric flow is more frequently from the southwest bringing more moisture to the ice sheet, particularly in the southern region (Mosley-Thompson et al., 2005). Except in summer (JJA), the simulation reflects very well the heavier precipitation along the ice sheet eastern slope and the diminished precipitation along the western slope during high NAO phases. This pattern has been also identified by Appenzeller et al. (1998). Significant positive correlations with the NAO are obvious in summer (JJA) in the northwest and in the east.

The temperature is anti-correlated with the NAO index everywhere and in every season; up to half of the temperature variability is explained by the NAO in winter (DJF). In summer (JJA), the sensitivity to the NAO is not significant (Table 4) in agreement with Hanna et al. (2007). Some NAO links with precipitation can also be found but they are less homogeneous in time and space. In an annual average and averaged over the ice sheet, the precipitation is not correlated with the NAO as in Hanna et al. (2006). Therefore the NAO is a good proxy for the Greenland winter temperature but does not explain the accumulation (winter snowfall) nor the melt (summer temperature) changes over the last 28 years. Beside, the last 40 years are characterized by large positive trends of NAO/AO indexes (Solomon et al., 2007) suggesting rather a cooling in Greenland and a warming in the Arctic region (Hanna and Cappelen, 2003; Goosse and Holland, 2005).
6 Discussion and conclusions

A 28-year simulation (1979–2006) of the GrIS shows an insignificant increase in solid precipitation (+0.4±2.5 km$^3$ yr$^{-2}$) but a significant and positive perturbation of the meltwater production (+7.9±3.3 km$^3$ yr$^{-2}$). The increasing snowfall offsets the run-off increase to give a significant SMB mass loss rate of −7.2±5.1 km$^3$ yr$^{-2}$. The contribution of changes in the net water vapour fluxes to the SMB variability is negligible (+0.02±0.09 km$^3$ yr$^{-2}$). The meltwater production has increased because the GrIS surface has been warming up by +2.4°C since 1979. More than 96% variance in the modelled surface mass balance total is explained by the summer (from 1 June to 31 August) temperature and the annual precipitation variability. A small part of the increasing liquid water supply comes from heavier rainfall (+0.2±0.2 km$^3$ yr$^{-2}$). Due to higher temperatures, the liquid fraction of total precipitation has been increasing. Snowfall shows negative trends along the ice sheet margin where the amount of liquid precipitation has been increasing. The temperature has increased because of higher net solar and infrared radiations. No significant changes in either latent or sensible heat fluxes occur. The SWD flux does not show variations during these 28 years except negative anomalies in 1983 and 1992 due to volcanic eruptions (El Chichón and Mount Pinatubo). The SWDn flux has increased because the albedo has been decreasing. Lower accumulation rates in winter could explain this. Indeed, thin snow packs by the end of the winter lead to faster losses of winter snow mass and to higher degree day factors (i.e. higher solar radiation absorbed by the surface) for bare ice (with a lower albedo) in the ablation zone. But according to our results, winter snowfall has not changed. Therefore, it is rather resulting from the increasing melt which wets the snow and decreases the albedo. Besides, the SWDn flux has increased only in the zone where melting has increased while the warming is occurring everywhere on the ice sheet. It is clear however that the decreasing albedo amplifies in turn the warming-related melt increase by the well-known albedo-temperature positive feedback. Consequently, the GrIS warming is mainly explained by higher LWD fluxes. The warming is almost uniform over the ice sheet as infrared radiations increase, suggesting that it comes from an external forcing.

The melt has significantly increased because the GrIS has been warming up at the surface in the last decades due to higher LWD fluxes. These changes are significant and can not be explained by natural variability (e.g. the North Atlantic Oscillation). Therefore, they could be a response (in agreement with the conclusions of Hanna et al., 2007) to the GHG concentration increase induced by human activities since the beginning of the industrial era and the recent global warming related to it (Solomon et al., 2007). Higher GHG concentrations increase the incoming infrared fluxes and warm up the free atmosphere. Although the MAR radiative scheme includes the interannual fluctuations of gases/aerosols concentrations, the major temporal variability comes from its boundaries via the ECMWF (re)analysis which take into account the recent GHG concentration increase and the resulting global warming. The MAR simulated 500 hPa-temperature is 0.98 correlated with the one obtained by the (re)analysis and that shows an increase of +0.07°C yr$^{-1}$ since 1979. Finally, the correlation between the annual MAR 3m-temperature averaged on the GrIS and the global average temperature from the CRU data set (Brohan et al., 2006) is 0.66.

Since 1979, MAR simulates an increase of 102% of the freshwater flux into the ocean due to an acceleration of snow/ice melting at the GrIS surface. This increase occurs everywhere along the Greenland coast. Its maximum is found along the West coast (see Figs. 17 and 18). Integrated over Greenland (ice sheet and tundra), the 28-year
run-off rate shows a positive trend of $+8.2 \pm 3.5 \text{ km}^3 \text{ yr}^{-2}$ which is equivalent to a rate of global average sea level rise of $+2.3 \pm 1.0 \times 10^{-2} \text{ mm yr}^{-2}$. The 28-year average of the annual Greenland run-off is $407.2 \text{ km}^3 \text{ yr}^{-1}$ (sea level equivalent is $+113 \times 10^{-2} \text{ mm yr}^{-1}$). This flux reached $636.8 \text{ km}^3 \text{ yr}^{-1} = 2.02 \times 10^{-2} \text{ Sv}$ in the melt record year of 2003. We must add to this flux the glacier discharge and the basal melting flux which is normally considered as equal to the meltwater flux. Furthermore, increases in meltwater amount suggest an increase in glacier discharge due to the observed meltwater-induced ice sheet flow acceleration (Zwally et al., 2002). Once the ice starts to melt at the surface, lakes develop and ultimately discharge into crevasses down to the glacier base. Meltwater lubricates this base and, doing so, impacts glacier movement.

To conclude, this paper shows that the GrIS has been significantly losing mass since the beginning of eighties, by an increasing meltwater run-off as well as by a probable increased iceberg discharge into the ocean due the process found by Zwally et al. (2002). The global warming induced by human activities could explain these changes. As a result, it seems that increased melting dominates over increased accumulation in a warming scenario and that the GrIS will continue to lose mass in the future. The GrIS melting will have an effect on the stability of the thermohaline circulation (THC) and the global sea level rise. On the one hand, increases in the freshwater flux from the GrIS (glacier discharge and run-off) could perturb the THC by reducing the density contrast driving it. On the other hand, a melting of the whole GrIS would account for a global mean sea level rise of 7.4 m.

Appendix A

Uncertainty range given for the trend

The uncertainty range given for the trend of the SMB, run-off, . . . (plotted in Fig. 4) denotes two standard trend deviations (i.e. a significance of 95%) using the method described in Chapter 6.2 from Snedecor and Cochran (1971). It is computed from the time series plotted in Fig. 4 according to:

$$e_1 = \sum_i (\text{trend}(a_i) - a_i)^2$$  \hspace{1cm} (A1)

$$e_2 = \sum_i (y_i - \text{mean}(y_i))^2$$  \hspace{1cm} (A2)

$$\text{range} = \sqrt{e_1/((2006 - 1979 - 1) \times e_2) \times k}$$  \hspace{1cm} (A3)

where

- $a_i$ = time series of the variables plotted in Fig. 4
- $y_i$ = time series of the 28 years (1979, 1980, . . .)

$k=1.96$ to have a significant of 95%. ($k=1$ or $k=3$ for a 67% significant or a 99.5% significant respectively). The trend of a time series is significant if it is higher than its uncertainty range.

Acknowledgements. All major computations were realized with the computing resources of the Institut de Calcul Intensif et Stokage de Masse (CSIM) from the Université catholique de Louvain (http://www.cism.ucl.ac.be). The author would like to thank sincerely J.-P. van Ypersele for providing facilities during the writing of this paper. The comments and support from H. Gallée, M. Erpicum, J.-P. van Ypersele, F. Lefebre, W. Lefebvre were extremely valuable. Finally, the author also want to thank A. Prick for her precious spelling check in this manuscript.

Edited by: M. Van den Broeke
References


Janssens, I. and Huybrechts, P.: The treatment of meltwater re-


www.the-cryosphere.net/1/21/2007/


