Abstract. Rock glaciers are landforms that form as a result of creeping mountain permafrost which have received considerable attention concerning their dynamical and thermal changes. Observed changes in rock glacier motion on seasonal to decadal timescales have been linked to ground temperature variations and related changes in landform geometries interpreted as signs of degradation due to climate warming. Despite the extensive kinematic and thermal monitoring of these creeping permafrost landforms, our understanding of the controlling factors remains limited and lacks robust quantitative models of rock glacier evolution in relation to their environmental setting.

Here, we use a holistic approach to analyze the current and long-term dynamical development of two rock glaciers in the Swiss Alps. Site-specific sedimentation and ice generation rates are linked with an adapted numerical flow model for rock glaciers that couples the process chain from material deposition to rock glacier flow in order to reproduce observed rock glacier geometries and their general dynamics. Modeling experiments exploring the impact of variations in rock glacier temperature and sediment–ice supply show that these forcing processes are not sufficient to explain the currently observed short-term geometrical changes derived from multitemporal digital terrain models at the two different rock glaciers. The modeling also shows that rock glacier thickness is dominantly controlled by slope and rheology while the advance rates are mostly constrained by rates of sediment–ice supply. Furthermore, timescales of dynamical adjustment are found to be strongly linked to creep velocity. Overall, we provide a useful modeling framework for a better understanding of the dynamical response and morphological changes of rock glaciers to changes in external forcing.

1 Introduction

Rock glaciers and their dynamics have received much attention in permafrost research and beyond, most prominently by the International Panel on Climate Change (IPCC) in the context of impacts of a warming climate on high mountain permafrost (IPCC, 2014). Time series of rock glacier movement in the European Alps indicate that acceleration in permafrost creep in recent decades is related to an increase in ground temperatures (Delaloye et al., 2010; PERMOS, 2013; Bodin et al., 2015). Furthermore, multitemporal geomorphometric analysis has shown subsidence features and structural disintegration of alpine rock glaciers, which are indicative of landform degradation and destabilization (Kääb et al., 2007; Roer et al., 2008b; Bodin et al., 2010; Springman et al., 2013; Micheletti et al., 2015). Many studies have addressed the connection between mean annual air temperatures and rock glacier dynamics from a descriptive point of view (Ikeda and Matsuoka, 2002; Roer et al., 2005b; Delaloye et al., 2010; Springman et al., 2012) or have used modeling approaches to assess rock glacier dynamics (Jansen and Hergarten, 2006; Kääb et al., 2007; Springman et al., 2012). Most of these studies focus on the impact of air or ground temperature on rock glacier creep. Other authors stressed that rock glacier dynamics cannot solely be explained by temperature variations and should integrate flow and controlling environmental factors such as sediment supply dynamics and landform characteristics (Roer et al., 2005b; French, 2007; Frauenfelder et al., 2008). Rock glaciers have been defined as “lobate or tongue-shaped bodies of perennially frozen unconsolidated material supersaturated with interstitial ice and ice lenses that move down slope by creep as a consequence of the deformation of ice contained in them and which are, thus, features of cohesive flow” (Barsch, 1992, p. 176). Such
a definition includes information on form, material and process and, therefore, the observable rock glacier characteristics are influenced by sediment and ice input, permafrost conditions and the geomorphological setting, which in turn control rheology and landform geometry (Barsch, 1996). Very few studies have addressed rock glacier dynamics with such a holistic approach that includes rock wall retreat, sediment and ice dynamics, and climate variations to gain insight into the long-term evolution of rock glaciers (Olyphant, 1983; Frauenfelder et al., 2008) and model validation was hampered by restricted observational data.

Recent observations show signs of rock glacier destabilization such as acceleration, subsidence features and structural disintegration (forming of tension cracks) at several rock glacier landforms in the Swiss Alps (Kääb et al., 2007; Roer et al., 2008b; Delaloye et al., 2011; Lambiel, 2011; Springman et al., 2013; PERMOS, 2013; Kenner et al., 2014; Bodin et al., 2015). These studies indicate that various factors can lead to such degradation but a common triggering for all the cases has not been identified. These potential factors are most likely connected to the complex combination of the local topography, the thermal state of the permafrost (climate-induced response), the existence and intrusion of liquid water and/or variations in the sedimentation regime affecting the sediment load during long-term landform evolution.

Numerous remote sensing techniques are available for acquiring data on permafrost creep (see Haebel et al., 2006, and Kääb, 2008, for an extensive summary), high mountain geomorphometry (Bishop et al., 2003) and high mountain sediment dynamics (Gärtner-Roer, 2012; Heckmann and Schwanghart, 2013; Müller et al., 2014a). This provides the necessary foundation for a holistic assessment strategy that includes the coupling of relevant landforms and processes and in which sediment supply rates can be quantified, ice volumes estimated and rock glacier rheologies derived (Frauenfelder et al., 2008; Gärtner-Roer and Nyenhuis, 2010).

Here we present such a holistic analysis approach to assess long-term rock glacier evolution and the impacts of variations in temperature, sediment and ice supply on rock glacier geometry and movement. We apply a numerical flow model to two rock glaciers in the Swiss Alps with different topographic, morphometric and rheological characteristics. The modeling is motivated by observations of topographic and kinematic changes for the two rock glaciers revealing signs of degradation as presented in this study. The aim of the modeling approach is to relate these changes to the long-term evolution and short-term adaptation of rock glacier systems to changing environmental factors and ultimately to a better understanding of the currently observed dominant controls of geomorphological changes. We thereby consider rock glaciers as an integral part of a coarse-debris cascading system in periglacial environments.

Figure 1 shows the theoretical concept of an idealized periglacial mountain slope with a corresponding rock glacier system and builds the conceptual basis for this study. Two main subsystems contribute to the temporal and topographical development of the rock glacier landforms: the upper headwall and talus slope system generate the sediments that are transported into the lower rock glacier system. Besides the sediment input, the rock glacier system is also controlled by the existence, generation and state of subsurface ice and permafrost creep (see Fig. 1). The two subsystems differ on the basis of several characteristics: topographic features, typical landform(s) and the dominating mass transport processes. Back-weathering of the exposed rock wall and resulting rockfall are the most effective mass wasting processes (e.g., Krautblatter et al., 2012; Müller et al., 2014a) and supply the entire system with sediment. Back-weathering rates and rock wall dynamics are strongly influenced by the ge-
ological structures, lithological conditions, the presence of moisture as well as the characteristics and dynamics of cleft ice, which are in turn thermally controlled (Hasler et al., 2012). The progressive accumulation of sediments and ice on an inclined surface at the foot of the rock wall under permafrost conditions leads to permafrost creep and the development of a rock glacier (Barsch, 1992; Haebler et al., 2006). The existence of ice and its properties within the sediment obviously plays an important role in controlling the rheology of the rock glacier and environmental changes influence erosion and transport processes that result in topographical and kinematic changes (White, 1973; Arenson et al., 2004; Haebler et al., 2006).

We transfer this conceptual approach into a numerical flow model that integrates the whole debris process chain and couples the different subsystems and related mass fluxes. It assumes a uniform sediment and ice input from the rock wall to an inclined surface, builds up a talus slope that is supersaturated with ice and then starts to creep as a viscous nonlinear media similar to ice. This rheological assumption has repeatedly been used to assess rock glacier kinematics (Wahrhaftig and Cox, 1959; Olyphant, 1983; Whalley and Martin, 1992; Barsch, 1996; Kääb, et al., 2007; Frauenfelder et al., 2008). A few studies (e.g., Olyphant, 1983; Wagner 1992; Leysinger Vieli and Gudmundsson, 2003; Frehner et al., 2015) have demonstrated that such a rheology can in principal be used in a numerical flow model for rock glaciers.

3 Recent observations of rock glacier change

The modeling work in this study is motivated by detailed observations of geometric changes of two rock glacier systems, both in Switzerland. We present in this section comprehensive new datasets of the two landforms: the well-studied Murtèl rock glacier in the Engadine and the rock glacier Huhh1 in the Turtmann valley. Both show changes in surface geometry and kinematic behavior but have distinctly different landform characteristics (see Table 1 for an overview).

In order to assess the controlling mechanisms of rock glacier evolution and potential degradation we use a “backward” approach: we quantify and discuss distinct observed changes in surface geometry and kinematics of the two rock glaciers, propose potential controlling forcing factors (sediment and ice input as well as ground temperature) and then assess these observations and related forcings with a numerical creep model.

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Murtèl rock glacier</th>
<th>Huhh1 rock glacier</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average thickness</td>
<td>30 m</td>
<td>12 m</td>
</tr>
<tr>
<td>Length</td>
<td>280 m</td>
<td>310 m</td>
</tr>
<tr>
<td>Slope</td>
<td>12°</td>
<td>27°</td>
</tr>
<tr>
<td>Age</td>
<td>~5000–6000 a</td>
<td>~600 a</td>
</tr>
<tr>
<td>Hor. velocity</td>
<td>0.06–0.13 m a⁻¹</td>
<td>0.75–1.55 m a⁻¹</td>
</tr>
<tr>
<td>Headwall area</td>
<td>74 687.1 m²</td>
<td>82 781.6 m²</td>
</tr>
<tr>
<td>Depositing area</td>
<td>45 931 m²</td>
<td>32 356 m²</td>
</tr>
</tbody>
</table>

3.1 Murtèl rock glacier, upper Engadine

The first rock glacier site is the well-studied Murtèl (Hoelzle et al., 2002; Haebler et al., 2006; Springman et al., 2012) situated below the northern face of Piz Corvatsch (3300 m a.s.l.) in the upper Engadine, in the southeastern part of Switzerland (UTM, 563 131, 5 142 001; zone 32T). The lithology mainly consists of granite and granodiorite. The density of the in situ rock types is based on values given in the literature with a density of 2650–2750 kg m⁻³ for granite and 2700–2800 kg m⁻³ for granodiorite (Tarbuck et al., 2011), and studies on back-weathering at this site have shown back-weathering rates of 2 mm a⁻¹ (Müller et al., 2014a). Murtèl is one of the best investigated rock glaciers and observations from this permafrost site have been discussed in great detail (see summary in Haebler et al., 1998). As part of the PERMOS network (Permafrost Monitoring Switzerland), parameters such as borehole temperatures, ground surface temperatures (GSTs) and horizontal velocity have been monitored since 1987 (Vonder Mühll et al., 2008). The borehole data have revealed a layered internal structure with a shear horizon at 32 m depth where almost all of the deformation takes place (Arenson et al., 2002; Springman et al., 2012). Attempts to determine the age of this rock glacier (Haebler et al., 1999; Laustela et al., 2003) obtained an age of 5000 to 6000 a as a minimum value (Haebler et al., 2003). These values were calculated from present-day surface velocity fields assuming constant environmental conditions over the rock glacier development (Kääb and Vollmer, 2000; Frauenfelder and Kääb, 2000; Haebler et al., 2003). The rock glacier is characterized by rather slow creep velocity (0.06–0.13 m a⁻¹) and is considered a thick and ice-rich landform with an average volumetric ice content of 60 % (Haebler et al., 1998; Arenson et al., 2002).

3.2 Huhh1 rock glacier, Turtmann valley, Valais

The second rock glacier is located in one of the hanging valleys of the Turtmann valley, a tributary of the Rhône valley in southern Switzerland (UTM 401 555, 5 115 642T; zone 32T). The valley’s lithology mainly consists of Palaeozoic gneisses...
and schists and based on this lithology rather constant backweathering rates of \(2\text{ mm a}^{-1}\) are expected (Glade, 2005; Krautblatter et al., 2012; Müller et al., 2014a). The valley stretches from 2400 to 3278 m a.s.l and is characterized by steep rock walls, talus cones, a glacier, several moraines of different ages and multiple active and inactive rock glaciers (Roer and Nyenhuis, 2007). The focus within this study lies on the rock glacier Huhh1, which can be considered a thin, moderately fast moving rock glacier (see Table 1). This site is also part of the PERMOS network and has undergone several scientific assessments (Rasemann, 2003; Roer, 2005; Nyenhuis et al., 2005). There is no direct subsurface information available but Gärtner-Roer (2012) used a semi-quantitative approach to derive the rock glacier thickness and sediment storage assuming an ice volume of 50–70 %. The age of the landform is estimated at 500–600 a using the same approach as Haeberli et al. (2003) and Kääb and Vollmer (2000), where the current velocity fields are assumed to be constant over the rock glacier evolution time. Therefore the age estimates can be seen as minimum ages.

### 3.3 Observations of rock glacier dynamics

Complementary to the PERMOS-related kinematic monitoring, we used a combination of remote sensing and terrestrial surveying methods to derive multitemporal elevation and displacement data in order to assess changes in geometry and creep.

Multitemporal digital elevation models (DEMs) derived from stereophotogrammetry and airborne laser scanning (ALS) are available for the analysis between the years 1996 and 2007 for the Murtèl rock glacier. Five high-resolution DEMs (also stereophotogrammetry and ALS) have been generated in this study for the Turtmann valley between the years 2001 and 2010; the technical details of these DEMs are given in Table 2. New elevation change maps are derived from differencing of the DEMs over the periods 1996 and 2007 for Murtèl and 2001 and 2012 for Huhh1. The limitations concerning processing, uncertainties and application of the different sensor systems are presented in Kääb and Vollmer (2000), Roer et al. (2005d), Roer and Nyenhuis (2007) and Müller et al. (2014b). The systematic error/trueness (Menditto et al., 2007) of the remote sensing data was corrected using the terrestrial geodetic survey points (tachymeter) as reference for the ALS and the ALS data as reference for the photogrammetric DEM data, as presented in Müller et al. (2014b). The spatial coverage of each reference dataset allowed us to establish a slope-dependent detection limit derived from the assessment ranging from 0.5 to 0.9 m (see also Müller et al., 2014b). The availability of numerous multisensoral datasets enabled stacking, investigating dense time steps and crosschecking products with different precisions (terrestrial survey, ALS, photogrammetry), which led to a high reliability of the DEM differencing and derived annual subsidence rates (Winsvold et al., 2016).
Table 2. Airborne and terrestrial remote sensing data available at the rock glacier sites.

<table>
<thead>
<tr>
<th>Data type</th>
<th>Murtèl</th>
<th>Huhh1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Airborne remote sensing</td>
<td>RC30 in 1996 (PERMOS)</td>
<td>HRSC-A in 2001; Otto et al. (2007)</td>
</tr>
<tr>
<td>laser scanning – ALS</td>
<td>ALS in 2003</td>
<td>ALS in 2007; Müller et al. (2014a)</td>
</tr>
<tr>
<td></td>
<td>RC30 in 2007 (PERMOS)</td>
<td>ADS 40 in 2010; Müller et al. (2014a)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>ADS 80 in 2012; Müller et al. (2014a)</td>
</tr>
<tr>
<td>Geodetic point surveys</td>
<td>2009–2015 (annually)</td>
<td>2001–2015 (annually)</td>
</tr>
</tbody>
</table>

Figure 3. The frequency distribution of annual vertical surface change (m a\(^{-1}\)) from DEM differencing in the talus slope–sedimentation area of the two rock glacier systems. Both systems show negative mean values (red lines). The black line refers to 0 m a\(^{-1}\) difference.

Additionally, kinematic data are available for both rock glaciers from yearly terrestrial geodetic surveys of approximately 20 points as described in PERMOS (2013) and Roer (2005). Horizontal and vertical changes are quantified annually with an accuracy of 1–2 cm. The vertical elevation change is obtained by subtracting the surface-parallel component of the vertical displacement from the total measured vertical displacement.

Based on the above DEMs, new elevation change maps have been derived for both rock glaciers and the subsystems of the main rock glacier body and contributing talus slope have been identified (Fig. 2). This analysis (over decadal time periods) showed distinct subsidence features of different magnitudes on the entire rock glacier, most pronounced in the deposition area (outline with green in Fig. 2) of the rock glacier. A more detailed assessment of the subsidence shows a general lowering of the entire surface of the rock glacier system of \(-0.02\) m a\(^{-1}\) for the Murtèl rock glacier and \(-0.09\) m a\(^{-1}\) for the Huhh1 rock glacier. The spatial analysis of the subsidence phenomenon depicts the strongest signal of annual lowering in the deposition area (talus slope–sedimentation area; see Fig. 3) with an overall average annual subsidence of \(-0.04\) m a\(^{-1}\) for the Murtèl rock glacier and \(-0.16\) m a\(^{-1}\) for the Huhh1 rock glacier. Such subsidence features, especially in the deposition area, have been interpreted as signs of permafrost degradation (Roer et al., 2008a; Springman et al., 2013; Bodin et al., 2015) and are assessed by the rock glacier evolution model in Sect. 6.2.4. These observed subsidence rates are calculated considering the uncertainties resulting from the DEM differencing (see Müller et al., 2014b). Additional vertical displacement data from terrestrial surveys conducted from 2001/2009 to 2015 corrected for slope parallel movement agree with the results from the DEM differencing.

Theoretically, subsidence features can result from surface lowering by ice melt (Phillips et al., 2009), reduced ice and sediment input, acceleration of the entire landform (potentially thermally induced, leading to a “creeping away” and thinning of the rock glacier from its feeding area) or, most likely, a combination of the above (Roer et al., 2005b).

Our elevation change data also show the continuing advance of the rock glacier front and the “furrow and ridge” structure. This shows that the rock glacier continues to be active although it is probably no longer fully connected to
its sediment source and therefore not in an equilibrium state with the current sedimentation and/or thermal state of the system.

4 Rock glacier evolution – modeling approach

We present here a quantitative rock glacier evolution modeling approach that is based on the conservation of mass and includes the entire debris process chain in high mountain environments (see Fig. 1).

4.1 Geomorphological setting

In order to initialize and evaluate the numerical model, it is necessary to derive geometric information about the headwall, talus slope and rock glacier. Therefore, the two rock glacier sites have been analyzed according to the concept introduced in Sect. 2 for their along flow geometry and the quantification of sediment input and sediment deposition. Geomorphological mapping in the field as well as interpretation of DEMs and orthophotos are used to identify the contributing headwall areas, deposition areas and rock glacier landforms (see Fig. 2). Surface features (e.g., slope, substrate) as well as velocity fields are further used to delimit the different subsystems (Kääb et al., 1998; Roer et al., 2005a).

The DEMs served as basis for the geomorphometric analyses to determine spatial dimensions, slope and surface geometry of the periglacial high mountain systems.

4.2 Rock glacier creep modeling approach

A 1-D time-dependent numerical flow model is used to simulate the evolution of the rock glacier surface, length and creep velocity along the center flow line based on a given sediment–ice input and rock glacier rheology. In this study we are not aiming to reproduce the exact evolution or small-scale geometric features of the two chosen real-world rock glaciers, but rather use the model to simulate the basic behavior of a rock glacier body creeping down a slope and investigate the first-order dynamic response of the geometry on changing external factors such as temperature and sediment supply. Specifically, we will investigate potential causes for the observed surface geometry changes (subsidence, front advance and velocity variations) as set out above (Sect. 3.3).

4.2.1 Rock glacier creep

For our study we therefore reduce the rheology of the rock glacier to a body of ice-bonded sediment that deforms and creeps like a nonlinear viscous material under the influence of gravity, as proposed already in 1959 by Wahrhaftig and Cox (1959) and applied similarly by Olyphant (1983) and Frauenfelder et al. (2008). This rheology can be described by a Glen type flow law (Glen, 1955) as typically used for glacier ice (Cuffey and Paterson, 2010) which relates the strain rate \( \dot{\varepsilon} \) nonlinearily to the stress \( \tau \):

\[
\dot{\varepsilon} \propto A \tau^n,
\]

where \( n \) is a flow law exponent that is typically between 2 and 3 for frozen material (Paterson, 2010) and \( A \) the rate factor describing the softness of the rock glacier material. Such a constitutive relationship has been applied and discussed in other studies on rock glacier creep (Olyphant, 1983; Whalley and Martin, 1992; Whalley and Azizi, 1994; Barsch, 1996; Azizi and Whalley, 1996; Kääb et al., 2007; Frauenfelder et al., 2008) and is further supported by results from borehole measurements on real-world rock glaciers and shear experiments in the laboratory on rock glacier material (including Murtèl rock glacier; Arenson et al., 2002; Kääb and Weber, 2004; Arenson and Springman, 2005; Frehner et al., 2015).

For simplification we assume the rock glacier material to be a homogenous mixture of ice and sediment, meaning the rheological parameters such as the rate factor \( A \), flow exponent \( n \) and rock glacier material density \( \rho_r \) do not change within the rock glacier body. This means that we exclude any internal ice melting and consider the active layer rheologically in the same way as the rock glacier material. However, from boreholes we know that the rheology within rock glaciers is variable with depth (Haeberli et al., 1998) and typically enhanced deformation in ice-rich shearing zones are observed, for example, in the case of the Murtèl rock glacier. Such shearing zones are typically near the bottom of the moving body of the rock glacier, where shear stresses are highest and temperatures the warmest, and thus they dominate the creep process. Consequently, potential variations in rheology in the material above are not substantially changing the nonlinear viscous creep behavior. The modeled flow is calibrated with observed surface velocities (see Sect. 4.3) and is dominated by the rheology of the material near the base and thus our modeling implicitly includes the shear zone in its vertically averaged rheology. In addition, the rheology within rock glaciers is generally poorly known and the assumption of a uniform rheology is therefore justified for studying the first-order controls of geometric changes.

We further simplify the problem to the case of an infinite sheet of uniform thickness that creeps down an inclined plane (Cuffey and Paterson, 2010, also known as the shallow ice approximation in glaciology) and thereby neglect longitudinal stress gradients. As our focus is the evolution of the surface and not the detailed stress field within the landform, according to Leysinger Vieli and Gudmundsson (2004) this approximation is justified even for relatively high length to thickness ratios such as occurring for rock glaciers. For this 2-S case along a center flow line, the vertical strain rate \( \dot{\varepsilon}_z \) is directly related to the shear stress \( \tau_{xz} \) through

\[
\dot{\varepsilon}_z = A \cdot \tau_{xz}^n,
\]

where \( x \) is the horizontal coordinate along the center flow line and \( z \) the vertical coordinate. The shear stress \( \tau_{xz} \) is then
given by the local surface slope $\frac{\partial s}{\partial x}$ and ice depth $d$: 

$$\tau_{sz} = \rho_r g \frac{\partial s}{\partial x} d,$$

where $\frac{\partial s}{\partial x}$ is the surface slope.

Integration of Eq. (2) over the rock glacier thickness results in a surface flow speed $u_s$ from deformation of the rock glacier material of

$$u_s = \frac{2A}{n+1} \left( \rho_r \frac{\partial s}{\partial x} \right)^n h^{n+1}$$

and accordingly a depth-averaged horizontal flow speed $\bar{u}$ of

$$\bar{u} = \frac{2A}{n+2} \left( \rho \frac{\partial s}{\partial x} \right)^n h^{n+1}.$$ 

Although this equation is in its form identical to the case of glacier ice (Cuffey and Paterson, 2010), for rock glaciers the flow exponent $n$ and the rate factor $A$ (referring to the material softness) are, due to the presence of debris and water within the ice, not necessarily the same (Moore, 2014) and may in reality thereby also vary with depth. From boreholes and laboratory experiment flow law exponents of rock glaciers have been found between $n = 1.9$ and $4.5$ (mean $n = 2.72$) and increase linearly with volumetric ice content $c_{ice}$ of the sediment (Arenson and Springman, 2005). For our relatively high ice contents (60 %) a value of $n = 3$ equivalent to the case of ice seems justified and has been used in earlier studies of Leysinger Vieli and Gudmundsson (2003) and Frauenfelder et al. (2008).

The rate factor $A$ is estimated from observed surface flow speeds by inverting Eq. (3) for $A$ but is known to be influenced by the material temperature but also by other factors such as the moisture and debris content (Cuffey and Paterson, 2010). Moisture content is known to vary with time and temperature (Moore, 2014; Monnier and Kinnard, 2016) but we do not explicitly include this in our model as such changes are poorly constrained. The temperature-related effect from moisture is, however, implicitly included by writing the rate factor of the rock glacier material as a product of the temperature-dependent part $A^*(T)$ and a scaling factor $f_A$ accounting for the influence of the debris:

$$A = A^*(T) \cdot f_A.$$ (6)

This approach is in agreement with known rheological investigations (Paterson and Budd, 1982; Arenson and Springman, 2005) and allows including a temperature forcing in our modeling experiments. For the temperature-dependent part we use two approaches. Firstly, as done in Kääb et al. (2007) we use the dependence on the temperature of pure ice, for which $A^*(T)$ increases exponentially with temperature (see Fig. 4; Paterson and Budd, 1982).

Secondly, and probably more realistic for rock glaciers, we follow the description based on shearing experiments of frozen debris material of Arenson (2005) which is given by

$$A^*(T) \propto \frac{2}{T+1}$$

for temperatures between $-1$ and $-4 \degree C$. Note that this second version is at warm temperatures above $-2 \degree C$, as expected for our two cases, more sensitive to temperature warming (Fig. 4). For both approaches the temperature dependence is applied at a reference temperature which refers approximately to the real mean annual temperature within the rock glacier body.

4.2.2 Thickness evolution

The evolution of rock glacier thickness $h$ and rock glacier surface elevation $s$ along the central flow line is calculated from the principle of mass conservation, which takes for the 1-D representation the following form (Oerlemans, 2001):

$$\frac{\partial h}{\partial t} = a_t - \frac{1}{w} \frac{\partial \bar{u} h w}{\partial x},$$

where $t$ is the time, $a_t$ is the rate of rock glacier material accumulation or removal at the surface ($>0$ for accumulation; in m a$^{-1}$), $w$ the rock glacier width and $\bar{u}$ the horizontal and vertically averaged flow speed. The geometry of the rock glacier bed transverse to flow is accounted for by assuming a parabolic valley that is prescribed and here assumed to be uniform along the flow. This allows the width of the rock glacier to vary with changing thickness; however, the effect of side drag is not explicitly included but it is implicitly contained in the scaling factor $f_A$ of the rate factor, which is calibrated on surface displacements.

The evolution of the rock glacier thickness and surface is calculated numerically on a regular grid with 10 m spacing.
along the center flow line. Using a standard implicit finite-difference scheme (Oerlemans, 2001), the evolution Eq. (8) is solved at each time step and for all grid points from the depth-averaged material flux \( \bar{q} = \mathbf{u} \cdot \mathbf{h} \cdot \mathbf{w} \) and the material input \( \alpha_t \) at the rock glacier surface.

### 4.3 Model input and calibration

#### 4.3.1 Model geometry

Approximate bedrock topographies are derived for both rock glaciers from the DEMs and geomorphic mapping (Sect. 4.1) and we assume the bedrock to be roughly parallel to the rock glacier surface. The shapes of the rock glacier beds are approximated to two sections of constant slope that are representative of the two respective rock glaciers. For both rock glaciers we mapped the first 150 m of the distance along flow as deposition area and apply there a spatially uniform material accumulation rate at the specified sedimentation rate and ice content, whereas further downstream no mass is added or lost at the surface. In the talus slope, where the material is accumulated, we use a slope of 37° (which is slightly below the angle of repose for unconsolidated talus slope material; Carson, 1977), which is steeper than on the rock glacier part (12° for Murtèl and 27° for Huhh1, see Table 4). The respective dimensions and slopes for the two rock glaciers are presented in detail in Table 1 and visualized in Fig. 5.

#### 4.3.2 Material input

The rock glacier material input rate \( \alpha_t \) at the surface is assumed to be positive and uniform on the talus slope and, if not mentioned otherwise, set to zero on the surface of the main rock glacier body. The latter means that in general no sediment or ice is lost or gained at the surface of the main rock glacier. The rock glacier material input at the surface is estimated from the sediment input from the headwall to the talus slope and its respective ice content, which is assumed to be constant in time. The total amount of sediment produced at the headwall is calculated from back-weathering rate and headwall area and is distributed equally over the deposition area (talus slope–accumulation area). Based on in situ measurements (Müller et al., 2014a) and previous studies (Glade, 2005; Krautblatter, 2012), a back-weathering rate of 2 mm a\(^{-1}\) is used, resulting in an annual sediment input over the entire talus slope of 0.006 m\(^3\) m\(^{-2}\) for Murtèl and 0.022 m\(^3\) m\(^{-2}\) for Huhh1. Together with the ice content of the material the accumulation rate of rock glacier material (sediment–ice mixture) is then calculated:

\[
\alpha_t = \frac{\alpha_s}{(1 - \chi_i)}. \tag{9}
\]

Based on field studies (Hoelzle et al., 2002) and previous approaches (Gärnter-Roer, 2012) we use an estimated ice content \( \chi_i \) of 60\% for both rock glaciers, which results in a rock glacier material input rate that is 2.5 times higher than the pure sediment input rate.

#### 4.3.3 Rock glacier density

We estimate the density of the rock glacier material \( \rho_r \) from the percentage ice content \( \chi_i \) and from the respective densities of ice \( \rho_i = 910 \text{ kg m}^{-3} \) and the debris material \( \rho_d = 2700 \text{ kg m}^{-3} \), which we assume stay constant in space and time:

\[
\rho_r = (1 - \chi_i) \cdot \rho_d - \chi_i \cdot \rho_i. \tag{10}
\]

#### 4.3.4 Estimating the rate factor \( A \)

Solving the equation describing surface ice flow from creep of a viscous material (Eq. 4) for the rate factor \( A \), we obtain

\[
A = A^* (T) \cdot f_A = \frac{(n + 1)u_k}{2h^n \tau_d} = \frac{(n + 1)u_k}{2h^{n+1} \rho_i g \frac{d_i^2}{27}}. \tag{11}
\]

Using observed surface flow speed data \( u_k \) we can then estimate the corresponding rate factor \( A \) (respective \( f_A \) for a given reference temperature and temperature dependence model) for both rock glaciers. These rate factor values are substantially lower than the values known for pure ice at similar temperatures (Paterson and Budd, 1982; –1.5°C), which probably reflects enhanced mechanical resistance from the sediment within the ice (Arenson and Springman, 2005).

### 5 Model experiments

The model is applied to the two selected rock glacier systems using the rock glacier-specific input parameters in Table 3 and the simplified geometries described in Sect. 4.

#### 5.1 Rock glacier buildup

The buildup experiment is documented for Murtèl in Fig. 6 (first 6000 a) and is qualitatively very similar for Huhh1 (shown in Supplement Figs. S14 to S25). The model starts with an “empty” topography of bedrock (bedrock topographies in Fig. 5). Initially, it builds up a homogenous sediment–ice body in the talus slope which starts to creep...
Figure 5. Observed and modeled rock glacier geometry after buildup. The along flow bed topography used in the model and the modeled and observed (from DEMs) rock glacier surfaces are shown. The vertical fine black lines mark the boundary between the deposition area (talus slope) and the main rock glacier lobe. Note that the model cannot replicate the exact geometry of the landform due to the various simplifications but shows good agreement in length and thickness of the rock glacier main body.

Table 4. Comparison of the observed (obs.) and modeled (mod.) rock glacier thickness and velocity for Murtèl and Huhh1 after 6000 years and 600 years, respectively.

<table>
<thead>
<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td>Length</td>
<td>280 m</td>
<td>300 m</td>
<td>310 m</td>
<td>240 m</td>
</tr>
<tr>
<td>Thickness</td>
<td>30 m</td>
<td>28 m</td>
<td>12 m</td>
<td>16 m</td>
</tr>
<tr>
<td>Horizontal velocity</td>
<td>0.06–0.13 m a$^{-1}$</td>
<td>0.06–0.09 m a$^{-1}$</td>
<td>0.75–1.55 m a$^{-1}$</td>
<td>0.63–0.79 m a$^{-1}$</td>
</tr>
</tbody>
</table>

and therefore advances once it is thick enough and the shear stress high enough, which occurs roughly after 600 a for Murtèl and 150 a for Huhh1. A rock glacier body is then generated to a characteristic thickness while the front keeps advancing at a roughly constant rate. This continuing advance is a direct result of constantly adding mass at the top while no mass is removed through melting. Further, the growth and geometry change of the rock glacier landform mainly occurs through moving the rock glacier forward at the front. The modeled advance rate is slightly below the surface speed of the main rock glacier body. After a run time of 6000 a for the Murtèl rock glacier and 600 a for Huhh1, which correspond to the ages of the landforms estimated earlier, we obtain geometries (lengths and thicknesses) that are very close to ones currently observed (Fig. 5 and Table 4). The actual furrow-ridge structure of the landform cannot be replicated (Fig. 5) due to model design but the overall geometry is well reproduced.

The modeled surface velocities on the main rock glacier lobes range between 0.06 and 0.09 m a$^{-1}$ for Murtèl and between 0.63 and 0.79 m a$^{-1}$ at Huhh1, which is in good agreement with the observed values from long-term kinematic monitoring (see Table 1).

Note that the bedrock topography of the talus slope and rock glacier is assumed to be of constant inclination. We defined the first 150 m of slope as an idealized talus slope with an inclination of 37°, which we assumed to be the angle of repose for such unsorted and unconsolidated blocky material (Carson, 1977). The general inclination of the bedrock topography (see Table 1) below the rock glacier is derived from DEMs where we assume the bedrock to be parallel to the rock glacier surface (see Table 1). Figure 5 depicts the observed rock glacier front shapes and positions slightly differently from the modeled ones as the real bedrock geometries of the rock glaciers are more complex than the assumed uniform mountain slopes. Also, the idealized talus slopes differ from the observed geometries due to abovementioned simplification.

5.2 Perturbation modeling experiments

Starting with the rock glacier geometries from the buildup experiments (see Sect. 5.1), we investigate the impact of variations in temperature and material input on rock glacier dynamics. In a first phase we perform two distinctly different perturbation experiments: in the first we increase the temperature of the rock glacier body by 1°C (Sect. 5.2.1) and in the second independent experiment we completely switch off the material supply to the talus slope (Sect. 5.2.2). In a second step, we then combine these perturbations in temperature and sediment supply. Atmospheric warming is expected to influence both rock glacier temperatures and consequently creep, as well as the
Figure 6. Modeled evolution of surface geometry (a), absolute thickness (b), horizontal velocity (c) along the central flow line, terminus advance (d) and volume evolution (e) for the rock glacier buildup (first 6000 a runtime) and for the successive temperature perturbation experiment (temperature increase of 1°C, with −1.5°C reference temperature). The black line shows the state of the system before the temperature step change at 6000 a. The lines are plotted at 100 a time intervals.

production of sediment and incorporation of subsurface ice, but quantification of the latter is highly uncertain (Gruber, 2004; Fischer et al., 2010; Ravanel and Deline, 2011; Schneider et al., 2012). We therefore run varying scenarios for the sediment and ice input with the zero sediment supply being at the extreme end of the spectrum.

For the temperature experiments the chosen step temperature increase of 1°C in the rock glacier depicts a potential warming scenario which roughly refers to a 2°C warming in GST for a fixed position at the permafrost base. The 1°C subsurface warming is also consistent with current and expected future subsurface warming trends based on borehole observations (PERMOS, 2013) and modeling results in the next 50 a in the Swiss Alps (Marmy et al., 2015).

Assuming relatively warm reference rock glacier temperatures between −1 and −2°C, as observed in the European Alps, the Arenson and Springman (2005) temperature dependence gives an increase of the rate factor by a factor of 1.4 to 2.7 (Table 5) for a 1°C warming. The Paterson and Budd (1982) temperature relation, however, shows almost no
shows a distinct thinning of up to 0.02 m a−1. As a result of the enhanced mass transport, the landform also
low lines), which then decays with time (orange to red lines).
rate factor causes an immediate speedup in horizontal flow of the entire landform by a factor of about 2 (Fig. 6c, yel-
lar temperature increase. If not indicated otherwise, we use the Arenson and Springman (2005) relation in the temperature warming experiments.
The results for the simple temperature and sediment experiments are presented in the following section only for Murtèl rock glacier but the results are qualitatively similar (although of higher absolute magnitude) for the Huhh1 rock glacier. The more complex and realistic experiments combining variations in temperature and sediment supply are presented for both rock glaciers later in Sect. 5.2.3.

5.2.1 Temperature experiment

In a first experiment, a step temperature increase of the entire rock glacier body of 1 °C is applied after rock glacier buildup (at 6000 a), while the sediment supply is held constant. The reference temperature of the rock glacier is set at −1.5 °C which results in a rate factor increase by a factor of 1.7.

Figure 6 shows the modeled response of the surface geometry, landform thickness and horizontal surface velocity of the Murtèl rock glacier along the central flow line. For reference, the black line in Fig. 6 shows the state of the rock glacier just after buildup (6000 a), immediately before the temperature step change is introduced. The increase in the rate factor causes an immediate speedup in horizontal flow of the entire landform by a factor of about 2 (Fig. 6c, yellow lines), which then decays with time (orange to red lines). As a result of the enhanced mass transport, the landform also shows a distinct thinning of up to 0.02 m a−1 in the upper part of the rock glacier and on the talus slope (Fig. 6b). At the front the rock glacier continues to thicken and consequently advance, but at accelerated rates as a consequence of enhanced flow speeds (Fig. 6d). With time, the creep velocity, advance rate and thinning reduce and approach stable values again after about 1000 a for Murtèl. We term in the following the time it takes for this readjustment the “adjustment time”. This new state after dynamic adjustment is, apart from the advancing front, stable and characterized by a slightly faster creep velocity and a thinner rock glacier body in order to transport the constant material supply from up-

<table>
<thead>
<tr>
<th>Rock glacier reference temperature</th>
<th>Change in rate factor A for Arenson and Springman (2005) from a 1 °C warming</th>
<th>Change in rate factor A for Paterson (1982) from a 1 °C warming</th>
</tr>
</thead>
<tbody>
<tr>
<td>−2 °C</td>
<td>1.396 · A</td>
<td>1.254 · A</td>
</tr>
<tr>
<td>−1.5 °C</td>
<td>1.705 · A</td>
<td>1.253 · A</td>
</tr>
<tr>
<td>−1 °C</td>
<td>2.718 · A</td>
<td>1.252 · A</td>
</tr>
</tbody>
</table>

dependence on rock glacier temperature and increases only by factor 1.25 with a 1 °C temperature increase. If not indicated otherwise, we use the Arenson and Springman (2005) relation in the temperature warming experiments.

5.2.2 Sediment experiment

In a second set of experiments, the influence of variations in sediment and ice supply is investigated by varying the material input $a_r$ but keeping the rock glacier temperature constant. Since there are no empirical data on the impact of temperature increase on sedimentation and ice accumulation rates, a range of changes in material supply rates has been explored.

Figure 7 shows the modeled response for an extreme example in which the ice and sediment input is completely switched off after rock glacier buildup (at 6000 a). The results show that the rock glacier continues to creep down-slope and advance but with reduced velocities that start to decrease from upstream. This slowdown is related to a thinning, reduced slope and driving stresses in the upper part of the rock glacier as the downstream flowing mass is no longer fully replaced by accumulation of material on the talus slope. The rock glacier body essentially creeps downstream without any mass added or removed, which is reflected well in the constant volume with time (dotted line in Fig. 7e). The advance rates thereby decrease at relatively low rates. The upper parts of the rock glacier react immediately to the change of material input as this is where the sedimentation is taking place. Note that the maximal thinning rates are only as high as the former material accumulation rate (in case of Murtèl 0.006 m a−1, for Huhh1 0.022 m a−1).

Experiments with different perturbations in material input rates show qualitatively similar changes but of reduced magnitude (Supplement Figs. S2 to S13) and are also evident in differing advance and volume growth rates (Fig. 7d and e).

5.2.3 Combined experiment

As atmospheric warming is expected to influence both rock glacier temperatures as well as ice and sediment production, we thus perform a third set of experiments in which we combine the above perturbations.

Twelve scenarios were run for each rock glacier assuming three different initial thermal states of each rock glacier (see Table 5), a potential warming of 1 °C and four different
scenarios concerning the material input (see Table 6). The corresponding results are shown in the Supplement.

In Figs. 8 and 9 we show detailed results for both Murtèl and Huhh1 rock glacier for one representative perturbation experiment in which we used a reference rock glacier temperature of \(-1.5\,^\circ\text{C}\), an increase in temperature of \(1\,^\circ\text{C}\) (corresponding to a rate factor increase by factor 1.7; Table 5) and a decrease of material input to 40\% of the original value. We assume that warming and subsequent thawing of permafrost in rock walls will lead to an increase in sediment production in the short term but is expected to attenuate in the long term (Krautblatter et al., 2013). Therefore we keep the material input from the rock wall constant but reduce the ice contribution to the total material influx.

Figures 8 and 9 illustrate the evolution of surface geometry and horizontal velocities along the central flow line of Murtèl and Huhh1 rock glacier, respectively. This combined experiment shows an upstream thinning of the “initial” landform in the subsequent years (Figs. 8a and 9a) and a substantial increase in horizontal velocities (Figs. 8b and 9b). The maximum thinning rates occur within the first few decades of the experiment and amount to 1.6 cm a\(^{-1}\) for
Figure 8. Modeled evolution of absolute thickness (a) and horizontal velocities (b) of the Murtèl rock glacier introducing a 1 °C temperature increase (1.7 times increase in rate factor) and a reduction in material input to 40% after the rock glacier buildup (6000 a, black line). The black lines in all plots depict the state of the rock glacier as shown in Fig. 5 before the perturbations were introduced. The lines are plotted at 100 a time steps.

Figure 9. The evolution of absolute thickness (a) and horizontal velocities (b) of the Huhh1 rock glacier introducing a 1 °C temperature increase (1.7 times increase in rate factor) and 40% of the initial material input after rock glacier buildup (600 a, black line). The black lines in all plots depict the state of the rock glacier as shown in Fig. 6 before the perturbations were introduced. The lines are plotted in 10 a steps.

Murtèl and 6 cm a⁻¹ for Huhh1 (see Fig. 11). A new stable geometry with advancing front is successively approached, again within adjustment times of roughly 1000 and 100 a for Murtèl and Huhh1, respectively. The final thickness and velocities of the main rock glacier body are, however, very close to the initial values.

Figure 10 shows the more detailed temporal evolution of geometry and creep velocity at three distinct positions on both rock glaciers. The rock glaciers keep advancing throughout the simulation, with initially slightly enhanced rates caused by the temperature increase and a successive slight slowing down caused by the reduced material accumulation rates. The adjustment times of Murtèl rock glacier are much lower compared to Huhh1, which was also shown by the simple perturbation experiments.

The additional combined experiments with a 1 °C temperature increase but variable reference temperatures and varying sediment supply rates show qualitatively similar geometric and kinematic responses (see Supplement Figs. S1–S24).

5.2.4 Subsidence

The sensitivity of the dynamic response to the initial temperature and to the temperature-dependent model has been further analyzed for the combined perturbation (1 °C warming, 60% reduction in material input) in a sensitivity modeling study (for detailed results see Supplement). As subsidence is
one of the observable quantities from repeated DEM analysis on real rock glaciers, we summarized the results in terms of maximum thinning rates in Fig. 11.

For the Paterson and Budd (1982) temperature relation, thinning rates are almost independent of the reference rock glacier temperature, but they increase with a reduction in material supply and reach maximum thinning rates of 1.8 and 6.5 cm a$^{-1}$ for Murtél and Huhh1, respectively. When using the Arenson and Springman (2005) temperature model, thinning rates strongly increase towards warmer rock glacier reference temperatures, reaching maximum values of 3.4 and 12.5 cm a$^{-1}$ for Murtél and Huhh1, respectively.
Table 6. All combined experiments. The creep rate change is implemented by increasing the rate factor $A$ (Eq. 6) and the change in material accumulation by varying the accumulation rate $a_t$ (Eq. 9).

<table>
<thead>
<tr>
<th>Model run</th>
<th>Creep rate change</th>
<th>Accumulation change</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.4 $\cdot$ A and 0 $\cdot$ Acc</td>
<td>1.4 $\cdot$ A</td>
<td>0 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>1.4 $\cdot$ A and 0.4 $\cdot$ Acc</td>
<td>1.4 $\cdot$ A</td>
<td>0.4 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>1.4 $\cdot$ A and 1 $\cdot$ Acc</td>
<td>1.4 $\cdot$ A</td>
<td>1 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>1.4 $\cdot$ A and 2 $\cdot$ Acc</td>
<td>1.4 $\cdot$ A</td>
<td>2 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>1.7 $\cdot$ A and 0 $\cdot$ Acc</td>
<td>1.7 $\cdot$ A</td>
<td>0 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>1.7 $\cdot$ A and 0.4 $\cdot$ Acc</td>
<td>1.7 $\cdot$ A</td>
<td>0.4 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>1.7 $\cdot$ A and 1 $\cdot$ Acc</td>
<td>1.7 $\cdot$ A</td>
<td>1 $\cdot$ $a_t$</td>
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<tr>
<td>1.7 $\cdot$ A and 2 $\cdot$ Acc</td>
<td>1.7 $\cdot$ A</td>
<td>2 $\cdot$ $a_t$</td>
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<td>2.7 $\cdot$ A and 0 $\cdot$ Acc</td>
<td>2.7 $\cdot$ A</td>
<td>0 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>2.7 $\cdot$ A and 0.4 $\cdot$ Acc</td>
<td>2.7 $\cdot$ A</td>
<td>0.4 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>2.7 $\cdot$ A and 1 $\cdot$ Acc</td>
<td>2.7 $\cdot$ A</td>
<td>1 $\cdot$ $a_t$</td>
</tr>
<tr>
<td>2.7 $\cdot$ A and 2 $\cdot$ Acc</td>
<td>2.7 $\cdot$ A</td>
<td>2 $\cdot$ $a_t$</td>
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</table>

6 Discussion

6.1 Modeling approach and rock glacier buildup

Based on a continuum approach, our numerical model couples observed sediment input rates and the rock glacier creep process in order to simulate the evolution of creep velocities and surface geometry as well as their dynamic interactions. This quantitative approach of coupling the relevant subsystems (headwall, deposition area and rock glacier), although highly simplified, was successful in building up the observed rock glacier geometries and related kinematics (horizontal velocities) within the expected timescales (Table 1). The basic dynamic behavior of a continuously advancing rock glacier body is well reproduced, while the thickness of the main body remains roughly constant.

The modeling of rock glacier buildup shows that besides topographical factors such as slope, the long-term advance rates and horizontal velocity are predominantly controlled by the rates of material accumulation and rock glacier rheology, whereas the thickness of the main landform seems less sensitive to material supply rates.

The match of observed to modeled velocities and thicknesses should, by model construction, be expected (for similar surface slopes) given that the rate factor $A$ and therefore the viscosity of the rock glacier material has been derived from such observed quantities (Eq. 11), but the agreement supports our modeling approach. More importantly, the material input rates and buildup times are fully independent estimates and it is therefore not necessarily obvious to get the right rock glacier geometry at the prescribed time.

Our modeled constant advance rates and consistency between modeled and previously estimated rock glacier buildup times further supports the method of back-calculating rock glacier age from current surface velocities (Frauenfelder and Kääb, 2000; Kääb and Vollmer, 2000; Haeberli et al., 2003). Even for the case of temperature perturbations, advance rates of the front do not substantially change in the long term and thus this “dating” methods seem still appropriate for alpine rock glaciers. Advance rates are in the long term, however, affected by changes in material supply rates. It remains to note that it is actually the vertically averaged velocity, and not the surface velocity, that should match the advance rates. Our modeled advance rates (derived from an assumed rheology with $n = 3$ in Eq. 5) corresponds in general to four-fifths of the surface velocity (e.g., modeled surface velocity on the main body of 0.065 m a$^{-1}$ and an advance rate of 0.054 m a$^{-1}$ for Murtel rock glacier). Consequently, using surface velocities in back calculations of rock glacier age may overestimate the age. For many real-world rock glaciers (including Murtel), rock glacier movement is dominated by deformation in a shear zone near the base and thus surface and vertically averaged creep is almost identical.

Strong simplifications have been made for our modeling approach such as using a homogenous sediment–ice body of uniform temperature and rheology and a spatially uniform and temporally constant material input. The successful rock glacier buildup therefore supports the idea that despite such simplifications rock glacier dynamics and evolution can be reduced to our simple model approach, which is based on the historic concept of Wahrhaftig and Cox (1959) and confirms earlier numerical modeling approaches of Olyphant (1983) and Frauenfelder et al. (2008).

The nonlinear viscous Glen type flow law used here is also supported by laboratory experiments (Arenson and Springman, 2005) and field observations from boreholes (Arenson et al., 2002). However, in reality the involved flow law parameters are, unlike the assumptions of our model, rarely constant in space and time. The flow law exponent $n$ has been found to increase with ice content (Arenson et al., 2002; Arenson and Springman, 2005) and rock glacier creep is mostly dominated by relatively thin shear layers with reduced viscosity (Hoelzle et al., 2002; Haeberli et al., 2006; Buchli et al., 2013). A more complex rheology of ice-debris mixtures could in theory and should in the future be included in rock glacier creep models, but currently there is very limited quantitative, field-based information available to constrain more complex constitutive relationships. Especially the role of moisture and the existence of unfrozen water appears to have a strong impact on the properties ice–debris mixtures as temperature nears the melting point and need to be further addressed (Moore, 2014) in establishing an adapted flow law for rock glaciers. This becomes increasingly more complex as an expected warming will not only influence the rheological properties of the ice itself but also change the ratio of ice and debris by reducing the volumetric ice content. A new ice–debris proportion will alter the viscosity of the rock glacier in a spatially heterogeneous manner because melting effects have been shown to be spatially diverse (Arenson and Springman, 2005; Monnier and Kinnard, 2010).
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Moisture variations due to precipitation events have been shown to impact rock glacier rheology in the short term down to a few days (Wirz et al., 2016), whereas the impact of a changing ice–water proportion is assumed to show its consequences in the long term. Nevertheless, due to the fact that the creep is dominated near the base within our model and that we have calibrated our model parameters to observed geometry and velocities, we do not expect the general dynamical behavior and involved timescales to be substantially different for other rheological parameter choices. We see our highly reduced approach also as an advantage for identifying the most essential controls and processes in rock glacier evolution.

In our approach the geomorphological mapping of the different subsystems, the quantification of sediment input rates, the ice content and the horizontal velocities are the crucial observational constraints and sufficient to set up a model of rock glacier evolution. However, the simplicity of the model design does not, by construction, allow reproduction of the exact small-scale features such as ridges and furrows of the two chosen real-world rock glaciers (Frehner et al., 2015).

6.2 Dynamical adjustment to external forcing

The perturbation modeling experiments of applying a sudden change in sediment input, material temperature or a combination of the two provide useful insights into the dynamical and geometric adjustment of rock glaciers to changes in external forcing and therefore also into potential mechanisms that explain observed rock glacier degradation.

The two types of perturbation experiments show similarities but also clear differences in the dynamic response. Both an increase in the rock glacier temperature as well as a reduction in material input lead to a thinning of the rock glacier and the talus slope, whereas the front keeps advancing through thickening. Although the thinning is caused by different mechanisms (lack of material supply from the rock wall or a runaway of mass through creep acceleration), from an observational point of view the two forcing mechanisms are difficult to distinguish. Importantly, the modeling shows a pronounced thinning occurring in the upper parts of both rock glacier systems (deposition area–talus slope).

The response in horizontal velocities are, for the two types of perturbations, distinctly different. A reduction in material supply results in a decrease of creep velocities from the top, whereas the temperature increase leads to an immediate acceleration of the entire landform, although in the long term the velocities return to almost pre-perturbation conditions (see Figs. 6c and 7c). The temperature experiments show a brief increase in the advance rates in the rock glaciers, but they subsequently return to similar rates as before the perturbation. This occurs in contrast with a continuous reduction of the advance rate during the decreased sediment supply experiment. Therefore, temperature changes within the rock glacier show a strong impact on short-term velocity variations whereas changes in the material input determine the long-term advance rates and geometry. Similar experiments by Olyphant (1983) and Frauenfelder et al. (2008) focused only on combined experiments and could therefore not address the impact of the individual forcings.

6.2.1 Dependence on rock glacier properties

Irrespective of the type of experiments, the absolute magnitude in response (velocity change, thickness change or advance rate) is very different for the two rock glaciers. Relative to the initial quantities, however (pre-perturbation velocity, thickness or advance rates), the dynamic changes are for both rock glaciers very similar (Fig. 10). This means that we should expect dynamic changes of rock glaciers to be scalable by their geometric (thickness) and kinematic characteristics (flow speed and advance rate). This scalability is also in good agreement with the observational dataset of multiannual creep variations of rock glaciers in the Swiss Alps (PERMOS, 2013). These show very similar normalized horizontal velocity variations as a potential response to air temperature changes despite their distinctly different characteristics (Delaloye et al., 2010 and PERMOS, 2013). Recent continuous observations of creep velocities on rock glaciers in the Matter Valley in the Swiss Alps confirm this finding even for seasonal timescales (Wirz et al., 2016).

The modeled short-term increase in horizontal velocity for a 1 °C warming in rock glacier body is also consistent with the observed speedup in rock glacier creep of about 300 % in the year 2003/2004 with exceptional snow conditions and a very warm summer (Delaloye et al., 2010).

6.2.2 Temperature dependence

Our temperature perturbation experiments assume an immediate warming of the entire rock glacier due to an increase in air temperature and consequently GST. This is, of course, an oversimplification because the vertical heat transfer depends on the energy balance at the surface and heat transport processes and thermal properties of the rock glacier material (Hanson and Hoelzle, 2004). Heat transfer processes should potentially be implemented in future studies (Kääb et al., 2007; Scherler et al., 2014). Hence we consider our modeled warming rather as a simple way to investigate the sensitivity to temperature increase.

For relatively thin rock glaciers such as Huh1, a climatic warming could affect the whole rock glacier thickness in timescales of a few years to decades (Marmy et al., 2015). For thicker rock glaciers such as Murtël, it could take several decades to centuries for the temperature change to reach the base where most of the deformation actually occurs. This implies that thin, and consequently steep and fast, rock glaciers should be more sensitive to warming from the surface.

The sensitivity to temperature warming is also enhanced for relatively warm rock glaciers (with temperatures only a
few degrees below freezing), considering the most realistic
model for temperature dependence of rock glacier rheology
by Arenson and Springman (2005). At −1.0 °C rock glacier
temperature, a warming of 1 °C results in a 2.7 times in-
crease in the rate factor (and hence creep velocity) whereas
the same warming at −2 °C results only in a 1.4 times higher
rate factor. Observed rock glacier temperatures in the Swiss
Alps indicate already relatively “warm” temperatures (close
to zero degrees) and show a tendency for further warming
(Permos, 2013). Such a warming would further amplify
the response in acceleration. In contrast, when using a tem-
perature dependence of pure ice (Paterson and Budd, 1982),
as done in an earlier attempt of modeling the impact of tem-
perature change on rock glacier creep (Kääb et al., 2007),
the sensitivity of creep to temperature warming is smaller (a
1 °C warming results in only a 1.25 times increase in rate fac-
tor) and does not additionally increase towards warmer rock
 glacier temperatures (Fig. 4). Thus, the impact of warming on
creep acceleration could be bigger than previously expected.

6.2.3 Adjustment timescales

The modeling shows that the “adjustment timescales” in
thickness and advance rates are for the faster and steeper
Huhh1 rock glacier with 100 a, an order of magnitude
faster than the 1000 a of Murtèl rock glacier (Figs. 6d and
7d). While in the literature such differences in adjustment
timescales have qualitatively been linked to the general rhe-
ology and mass turnover, the controlling factors remain un-
quantified. A comparison to theoretical considerations based
on the kinematic wave theory developed by Nye (1963) can
be made for the material supply experiment. Besides the
change in material supply rate, the thickness adjustment de-

dends mainly on the traveling wave speed of the thickness
perturbation and on its diffusion. According to Nye (1963;
and see also Hooke, 2005) the traveling wave speed \(v_0\) is
given by a multiple of the rock glacier flow speed and specif-
ically

\[ v_0 = (n + 2) \cdot u_s. \] (12)

The diffusion of the thickness perturbation is proportional to
the diffusivity which is given by

\[ D_0 = \frac{n \cdot q}{\alpha} = \frac{n \cdot \pi h}{\alpha}. \] (13)

where \(q\) is the ice flux and \(\alpha\) the surface slope. For Murtèl
and Huhh1, this results in diffusivities of 30 and 53 m² a⁻¹,
which are as a result of very small creep velocities and low
thicknesses much lower compared to diffusivities of pure-ice
glaciers.

Following Johannesson et al. (1989; see also Hooke,
2005, p. 376) the related adjustment timescales of thickness
changes to expand over the whole rock glacier lobe then de-
pend on a propagation timescale \(T_p\) and a diffusion timescale
\(T_d\). The propagation timescale is given by

\[ T_p = \frac{L_0}{v_0} = \frac{L_0}{(n + 2) \cdot u_s}, \] (14)

where \(L_0\) is the length scale of the rock glacier lobe. This
timescale is inversely proportional to the horizontal velocity
and consistent with our modeling results means that a factor
10 difference in creep velocity between Huhh1 and Murtèl
rock glacier translates into a factor 10 difference in adjust-
tment time. For \(n = 3\), lengths of 300 and 250 m and creep
velocities of 0.07 and 0.6 m a⁻¹ for Murtèl and Huhh1, we
obtain adjustment timescales of 860 and 83 a, respectively.
These theoretical values agree in absolute and relative mag-
nitude well with our modeled estimates.

The diffusion timescale is given by

\[ T_d = \frac{L_0^2}{D_0}, \] (15)

which results in 3000 and 1200 a for Murtèl and Huhh1, re-
spectively, for the thickness perturbation to spread over the
entire landform and which is substantially longer than the
timescales derived above for the kinematic wave propaga-
tion. These diffusion timescales are also much longer com-
pared to pure-ice glaciers and are consistent with the per-
sistent occurrence of morphological features of ridges and
furrows on the surface of rock glaciers.

To conclude, the propagation timescale, and therefore the
horizontal velocity, is a simple and meaningful measure for
rock glacier “adjustment timescales”. The very similar ad-
justment timescales obtained for the different types of pertur-
bation experiments support the notion that this propagation
timescale \(T_p\) can be used as a general measure of adjustment
in creep dynamics to a step change in external forcing. Note
that the introduced adjustment timescale is not the same as
the “volume response time” for pure-ice glaciers for adjust-
ing to a new climate (Johannesson, 1989) and should not be
confused with a “reaction time” (time taken for a rock glacier
to show a detectable reaction on an external forcing).

6.2.4 Geometry change and subsidence

Regarding geometry, the modeled rock glaciers respond to
both warming and reduction in material input by a thinning of
the landform that is fastest and most pronounced in the depo-
sition area and in the upper parts of the rock glacier (Fig. 10).
The front and therefore the landform as a whole continues
to advance, although at slightly differing speeds depending
on the applied perturbations (see Figs. 7b and 10a), even
if the material input is completely halted. The perturbation
experiments can also be compared with the observed subsi-
dence data presented in Sect. 3 in order to investigate the
potentially controlling mechanisms of such geometry change.
The observations in Figs. 2 and 3 show a pronounced sub-
sidence in the lower deposition area and upper parts of the
rock glaciers of roughly $-0.05$ m a$^{-1}$ for the Murtèl rock glacier and $-0.16$ m a$^{-1}$ for Huhh1 rock glacier while the lower rock glacier lobe shows relatively small or unchanging thicknesses and an advancing front. Thus, the spatial patterns in modeled geometry changes agree well with the observations. The absolute maximum rates of modeled subsidence are for both rock glaciers between 2 and 10 times smaller than the observed rates depending on the perturbation. These modeled rates result from an immediate warming of 1 °C of the entire rock glacier body, which is a rather extreme scenario. Further, the possible maximum rates of thinning from a total switch off in material input rates are limited to their pre-perturbation absolute values (0.006 m a$^{-1}$ for Murtèl and 0.022 m a$^{-1}$ for Huhh1), which are also almost an order of magnitude smaller than the observed subsidence rates.

Thus, we conclude that thinning due to thermally induced acceleration and a reduction in material input are not sufficient to explain observed subsidence patterns at Murtèl and Huhh1 rock glacier and that melt of subsurface ice is additionally required for the observed volume loss. The process of landform thinning, especially in the upper parts of the rock glacier, has been described as a sign of degradation by Ikeda and Matsuoka (2002), Roer et al. (2008b) and Springman et al. (2013). However, subsidence through melt of subsurface ice remains poorly constrained through observations and our process understanding and models linking them to external forcing are still limited (Scherler et al., 2014) and therefore we did not include this process in our flow modeling. In future work, internal ice melt (as a function of temperature) could technically easily be included through a negative accumulation term in the surface evolution Eq. (8) and an adjustment of the mean density.

7 Conclusions

This study uses a numerical flow model based on the conservation of mass within the cascading transport system of coarse debris to simulate the long-term and current evolution of rock glacier surface geometry and velocity. For a given sediment–ice input and rock glacier rheology, the model is able to generate observed rock glacier geometries and creep velocities in realistic timescales for two distinctly different rock glaciers. It is also capable of reproducing the continuing advancing front through creep which is often observed for rock glaciers (Barsch, 1996).

Climatic changes, especially increasing temperatures, are expected to influence rock glacier dynamics in a profound way. Our modeling approach allows not only for investigating the impact of a direct warming of the rock glacier material by adjusting the rheology (rate factor) but also for including the influence of changes in material input consisting of sediments and ice. Changes in geometry and related kinematics in response to such external perturbations can thereby be modeled and contribute towards a better understanding of the evolution of rock glaciers. Note that effects of internal ice melt or noncontinuous deformations such as the formation of tension cracks are not included in the current version of the model. Our detailed analysis of such perturbation experiments and modeling sensitivity studies give the following insights on rock glacier dynamics:

Short-term changes in velocities and advance rates result from temperature variations, whereas long-term geometric adaptations (thickness and advance rates) are mainly influenced by material supply. We show that a 1 °C temperature increase in rock glacier temperature can result in a 1.5–3 time acceleration of horizontal velocity depending on the initial thermal state of the rock glacier.

Both rock glacier temperature increase and reduction in material supply lead to thinning, while for the latter the maximum thinning rates are limited by the pre-perturbation material supply rate.

Irrespective of the perturbation, the rock glaciers keep advancing and remain active although the thermal and sediment input conditions are not favorable for their longevity, which is consistent with field observations.

Rock glaciers react spatially and temporally variably to changes in environmental factors. Changes in temperature affect the entire landform but the impact of material input variations is most pronounced in the sedimentation area and upper parts of the rock glacier. Comparing the model scenarios for localized topographic adaptations (subsidence) introduced by warming and variations in sediment–ice supply to observed subsidence features shows that these controlling factors are not sufficient to explain the magnitudes observed for our two examples. This implies that other processes such as melting of subsurface ice are responsible for subsidence and need further investigation.

Although the absolute magnitudes in thinning and creep acceleration differ between the two rock glaciers, the changes relative to the initial thickness and creep velocity, respectively, are very similar thus indicating that changes scale with their geometric and dynamic characteristics.

Based on most recent models of rock glacier rheology (Arenson and Springman, 2005), rock glaciers close to 0 °C likely show much stronger reactions to thermal forcing than colder ones.

On the basis of our modeling and kinematic wave theory, we propose a typical “timescale of dynamic adjustment” to external perturbations that is given by the inverse of a few times the horizontal velocity of a rock glacier. This timescale explains the order of magnitude difference in dynamic adjustment of our two chosen rock glacier examples which amount to 1000 a for Murtèl and 100 a for Huhh1.

The modeling approach presented here might serve as a useful tool to determine the dynamic state of rock glaciers, their potential state of degradation and related forcing mechanisms. The growing amount of observations on geometric changes and rock glacier movements may thereby serve as important constraints for such model assessments and serve
as indicators for the recent changes affecting periglacial high mountain systems. Therefore, future monitoring strategies should specifically be designed to detect spatially heterogeneous geometry changes and aim at observing entire slope systems, in addition to focusing on single landforms.

8 Data availability

Data on rock glacier kinematics are available from the PERMOS office upon request (see http://www.permos.ch/data.html). The digital elevation models derived from the RC30 sensor system at Murtél rockglacier 1996, 2002 and 2007 are also part of the PERMOS dataset. The remaining DEMs are available upon request from the authors.

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