Abstract. Energy balance based glacier melt models require accurate estimates of incoming longwave radiation but direct measurements are often not available. Multi-year near-surface meteorological data from Storglaciären, Northern Sweden, were used to evaluate commonly used longwave radiation parameterizations in a glacier environment under clear-sky and all-sky conditions. Parameterizations depending solely on air temperature performed worse than those which include water vapor pressure. All models tended to overestimate incoming longwave radiation during periods of low longwave radiation, while incoming longwave was underestimated when radiation was high. Under all-sky conditions root mean square error (RMSE) and mean bias error (MBE) were 17 to 20 W m\(^{-2}\) and -5 to 1 W m\(^{-2}\), respectively. Two attempts were made to circumvent the need of cloud cover data. First cloud fraction was parameterized as a function of the ratio, \(\tau\), of measured incoming shortwave radiation and calculated top of atmosphere radiation. Second, \(\tau\) was related directly to the cloud factor (i.e. the increase in sky emissivity due to clouds). Despite large scatter between \(\tau\) and both cloud fraction and the cloud factor, resulting calculations of hourly incoming longwave radiation for both approaches were only slightly more variable with RMSE roughly 3 W m\(^{-2}\) larger compared to using cloud observations as input. This is promising for longwave radiation modeling in areas where shortwave radiation data are available but cloud observations are not.

1 Introduction

Energy balance studies on glaciers have shown that, on average, net radiation is usually the largest contributor to surface ice and snow melt (see summary in Hock, 2005). Examination of the individual radiative components reveals that incoming longwave radiation (also referred to as downward or downwelling longwave radiation) is by far the largest source of energy for melt, followed by absorbed shortwave (or global) radiation (Ohmura, 2001), which accounts for roughly a quarter of the total energy source for melt. Sensible heat flux normally provides the third largest energy source. The relative importance of incoming longwave radiation as a source of surface energy input, compared to shortwave radiation or turbulent heat fluxes, may vary as climate changes (Philipona et al., 2004), but it will remain a large contributor, especially in the higher latitudes, due to the seasonal dependence of shortwave radiation. Hence, its accurate modeling is of paramount importance in energy balance glacier melt modeling and assessing the response of glacier melt to climate warming.

Longwave radiative fluxes have generally received less attention than shortwave fluxes, partially due to difficulties and costs associated with accurate longwave radiation measurements, but also due to a void of measurable atmospheric parameters which longwave radiation is dependent upon, such as cloud cover (Aase and Idso, 1978; Müller, 1985; Marty and Philipona, 2000). Unlike shortwave radiation, incoming longwave radiation is not readily measured at automated weather stations, often being derived through combination of global and net radiation measurements or parameterizations, although the number of weather stations on glaciers equipped with longwave radiation instrumentation has increased during recent years (e.g. van den Broeke et al., 2004; Sicart et al., 2005, 2008; van de Wal et al., 2005; Hoch et al., 2007; Mölg et al., 2009).
The atmospheric flux of longwave radiation is emitted predominantly by clouds, water vapor, carbon dioxide and ozone. The flux varies mostly with the cloud amount and cloud optical depth, mean cloud emitting temperature, as well as integrated water vapor content (Marty et al., 2002). In mountainous areas longwave irradiance from the surrounding terrain may locally enhance irradiance and thus generate spatial variability in melt (Plüss and Ohmura, 1997; Sicart et al., 2006). Ideally, incident longwave radiative flux is modeled with physical models describing all emission and absorption processes in the atmosphere. However, such models are not applicable when vertical profile data of temperature and moisture are lacking. Hence, empirical relationships have been developed parameterizing incoming longwave radiation as a function of near-surface (e.g. 2-m screen-level) temperature and/or vapor pressure for clear-sky conditions, and in addition as a function of cloud fraction in the case of all-sky conditions. Use of standard meteorological measurements at near-surface level has proven sufficient since most incoming longwave radiation reaching the Earth’s surface is emitted from the lowest layers of the troposphere (Ohmura, 2001). Only few studies have compared different parameterizations on the same data set (e.g. Sugiita and Brutsaert, 1993; Pirazzini et al., 2000; Gabathuler et al., 2001; Iziomon et al., 2003), and most studies have focused on lowland station data. Also, much attention has been devoted to clear-sky longwave radiation, although cloudy conditions often prevail in mountainous, glacier environments.

The purpose of this study is to evaluate various commonly used parameterizations of incoming longwave radiation in a glacier environment. The parameterizations vary in form, physical basis and number of independent variables, which include near-surface air temperature, water vapor pressure and cloud fraction. Further, we attempt to calculate incoming longwave radiation without observations of cloud fraction by two methods. First we develop a parameterization for cloud fraction since existing models often include it as independent variable, although such observations tend to be scarce in a glacier environment. Cloud fraction is parameterized as a function of the ratio of observed incoming shortwave radiation and computed top of atmosphere shortwave radiation, and this parameterization is incorporated into the calculations of longwave incoming radiation. Second we bypass the need for cloud data by parameterizing the cloud factor, i.e. the increase in sky emissivity due to clouds, as a function of the same ratio. Our analysis is based on a detailed micrometeorological data set collected on Storglaciären, a small glacier in Northern Sweden, spanning four melt seasons.

2 Site description and data

Storglaciären is located in Northern Sweden (67°55′ N, 18°35′ E) comprising an area of ~3 km². Elevation ranges between 1120–1730 m a.s.l. Mean summer temperature (June–August, 1965–2003) at Tarfala Research Station located ~1 km from the glacier is −3.7°C (Radic and Hock, 2006). An automatic weather station was operated in the upper region of the ablation zone at approximately 1370 m a.s.l. during the 1998–2000 and 2002 melt seasons. A detailed description of measurements and instrumentation is found in Hock et al. (1999); important to this study are the observations of incoming longwave and shortwave radiation, near-surface air temperature and humidity and cloud fraction.

An Eppley Precision Infrared Radiometer was used to measure incoming longwave radiation. The instrument underwent “Swiss modification” at the World Radiation Center in Davos, Switzerland, which incorporates three dome thermistors separated by 120° and an elevation of 45°, rather than using a single thermistor as in the original instrument. Details are given in Philipona et al. (1995) who claim that the accuracy of the modified instrument is 2 W m⁻² compared to approximately 10 W m⁻² for the unmodified version. Shortwave radiation was measured by a Kipp & Zonen CM11 with a reported maximum uncertainty of 2% for hourly values; temperature and humidity were measured using a Vaisala HMP45D. This instrument reports temperature accuracy of ±0.3°C at 0°C; humidity accuracy is reported as ±3% (0<RH<90%) and ±4% (90<RH<100%) at 0°C. Temperature and humidity measurements were maintained at 2 m heights, while radiation measurements varied in height between 1–1.5 m above the glacier surface. All instruments mentioned above were artificially ventilated to reduce measurement errors. Measurements were logged once per minute from which hourly means were computed. The weather station was visited at least twice a week for most of the melt seasons. Manual sky observations were recorded by trained observers in the vicinity of the automatic weather station. Hourly cloud observations were performed, consisting of cloud fraction and cloud-base height categorized by three levels (high, middle, low).

3 Methods

3.1 Incoming longwave radiation

Incoming longwave radiation, \( L_{\downarrow} \), (W m⁻²) is generally expressed in terms of the Stefan-Boltzmann Law

\[
L_{\downarrow} = \varepsilon_{\text{eff}} \sigma T^4 = \varepsilon_{cs} F \sigma T^4
\]

(1)

where \( \varepsilon_{\text{eff}} = \varepsilon_{cs} F \) is referred to as the effective or apparent emissivity (Unsworth and Monteith, 1975) and generally varies between roughly 0.7 for clear skies to close to unity for completely overcast skies; \( \varepsilon_{cs} \) is the clear-sky atmospheric emissivity, \( F \) (always ≥1) is a cloud factor expressing the increase in \( L_{\downarrow} \) due to cloud emission compared to clear-sky conditions, \( \sigma \) is the Stefan-Boltzmann constant (5.67×10⁻⁸ W m⁻² K⁻⁴) and \( T \) is absolute temperature (K) at the reference height (here 2 m). Parameterizations
of \(\varepsilon_{\text{cs}}\) and \(\varepsilon_{\text{eff}}\) have been developed both theoretically and empirically (e.g. Ångström, 1916; Brunt, 1932; Swinbank, 1963; Marshunova, 1966; Idso and Jackson, 1969; Maykut and Church, 1973; Brutsaert, 1975; Satterlund, 1979; Yamanouchi and Kawaguchi, 1984; Konzelmann et al., 1994; König-Langlo and Augstein, 1994), a number of which will comprise the suite of parameterizations that are tested on Storglaciären data in this paper.

### 3.2 Emissivity parameterizations

Seven parameterizations of clear-sky emissivity are analyzed (Table 1). The number and type of independent variables range from zero to two, allowing a model intercomparison dependent upon the number and type of independent variable(s) used. Parameterization coefficients \((a, b)\) are fitted to the Storglaciären data making a proper inter-model analysis possible. Clear-sky analysis is performed when observed cloud fraction \(n \leq 1/8\), resulting in 318 h cases.

Three parameterizations for all-sky conditions are examined and listed in Table 2. The \(\varepsilon_{\text{eff}}\) parameterizations from Bolz (1949) and König-Langlo and Augstein (1994) are principally different from Konzelmann et al. (1994). The former two parameterizations keep the clear-sky component regardless of cloud fraction while the latter reduces it as a cloud fraction increases. Coefficients are fitted to the data using all observed cloud fractions \((n=0–1, N=2332)\), except for the coefficient \(a\) in the Konzelmann et al. (1994) parameterization; this coefficient corresponds to the overcast emissivity, \(\varepsilon_{\text{oc}}\), and was fit to all hourly data with \(n=1\) \((N=1198)\). Fitted Konzelmann et al. (1994) parameterization coefficients lie within the range reported in the literature (Konzelmann et al., 1994; Greuell et al., 1997; Klok and Oerlemans, 2002). The three \(\varepsilon_{\text{eff}}\) parameterizations and seven \(\varepsilon_{\text{cs}}\) parameterizations are combined for \(L_{\downarrow}\) calculations according to Eq. (1).

### 3.3 Parameterizing emissivity without cloud data

Observations of cloud cover, though vital to \(L_{\downarrow}\) calculations, are often unavailable in high-latitude glacier environments. We explore the possibility of circumventing the need of cloud observations by including an atmospheric transmissivity index, \(\tau\), defined as the ratio of incoming shortwave radiation, \(S_{\downarrow}\), to theoretically calculated top of atmosphere shortwave radiation, \(S_{\downarrow,\text{toa}}\), dependent upon latitude, time of day and season

\[
\tau = \frac{S_{\downarrow}}{S_{\downarrow,\text{toa}}}. \tag{2}
\]

High values are indicative of clear-sky conditions while low values suggest overcast conditions. Some limitations to using Eq. (2) to simulate atmospheric transmissivity are discussed in Sect. 4.3. Since \(\tau\) becomes less reliable as radiation amounts decrease, cases when solar zenith angle exceeded 80° or \(S_{\downarrow} < 15 \text{ W m}^{-2}\) are excluded; also any cases when the measurement site was topographically shaded as determined from a digital elevation model and solar geometry are excluded.

First, we derive a parameterization for hourly and daily mean cloud fraction as a function of \(\tau\) and substitute it for observed cloud fraction in the \(\varepsilon_{\text{eff}}\) parameterizations given in Table 2. Sicart et al. (2006) apply a similar atmospheric transmissivity parameterization for data from a high-latitude mountainous region.

Second, the relationship between \(F\) (Eq. 1) and \(\tau\) is examined to explore the possibility to use \(\tau\) directly without the intermediate step of computing a parameterized cloud fraction. We derive a parameterization for \(F(\tau)\) for hourly and daily \(L_{\downarrow}\) calculations, thereby eliminating the need for cloud fraction data as independent variable.

\(L_{\downarrow}\) calculations based on \(\varepsilon_{\text{eff}}\) parameterizations are compared with observations, and also compared to calculations using observed and parameterized cloud fraction. We use the root-mean square error (RMSE), an indication of the variability of a calculation about the observed value, and the mean bias error (MBE), a measure of the mean error for all calculations, to aid in identification of parameterization caveats.

### 4 Results and Discussion

#### 4.1 Clear-sky \(L_{\downarrow}\) calculations

Clear-sky emissivities \((\varepsilon_{\text{cs}} = L_{\downarrow}/\sigma T_{\downarrow}^4)\) obtained from all hourly data of \(L_{\downarrow}\) and \(T\) from Storglaciären when cloud cover fraction \(n \leq 1/8\) \((N=205)\) tend to scatter around 0.7, generally consistent with clear-sky emissivities in prior studies (e.g. Konzelmann et al., 1994; Marty and Philipona, 2000). Statistics for clear-sky \(L_{\downarrow}\) calculations using the seven \(\varepsilon_{\text{cs}}\) parameterizations are found in Table 1, indicating that all parameterizations show comparable performance. Correlation coefficients, \(r\), and RMSE range from 0.84 to 0.88, and 10 to 12 W m\(^{-2}\), respectively. Parameterizations that incorporate both \(e\) and \(T\), tend to have the smallest RMSE and MBE, except for the formulation by Marshunova (1966) which performs similarly well although it only includes vapor pressure as independent variable. The inclusion of atmospheric moisture leads to an improved parameterization performance, suggesting that vapor pressure has a larger relevance than temperature for parameterizing clear-sky \(L_{\downarrow}\). This reinforces the notion of water vapor being the most effective greenhouse gas. A scatter plot of calculated versus observed clear-sky longwave radiation is shown in Fig. 1 using the Konzelmann et al. (1994) parameterization as an example.

#### 4.2 All-sky \(L_{\downarrow}\) calculations

Table 2 gives the correlation statistics for the three tested all-sky emissivity parameterizations each adopting seven different clear-sky emissivity parameterizations. All combinations
resulted in a similar range of $L_\downarrow$ calculation statistics. RMSE varied between 17 and 20 W m$^{-2}$, approximately 5.5 to 6.5% of mean measured $L_\downarrow$, and MBE remained between −5 and 1 W m$^{-2}$. All $\varepsilon_{\text{eff}}$ parameterizations performed best when the Konzelmann et al. (1994) $\varepsilon_{cs}$ parameterization was implemented. Besides calculations using the Konzelmann et al. (1994) $\varepsilon_{\text{eff}}$ parameterization, including near-surface vapor pressure as independent variable in $\varepsilon_{cs}$ parameterizations

Table 1. Clear-sky emissivity, $\varepsilon_{cs}$, parameterizations ($T$ is temperature [K], $e$ is vapor pressure [Pa], both at screen-level) used in this study and coefficients ($a$, $b$) fitted to the Storglaciären data set. Statistics result from comparing observations to calculations of clear-sky incoming longwave radiation applying the below parameterizations to Eq. (1). $r$ is correlation coefficient, RMSE is root-mean square error (W m$^{-2}$) and MBE is mean bias error (W m$^{-2}$).

<table>
<thead>
<tr>
<th>Clear-sky parameterization ($\varepsilon_{cs}$)</th>
<th>Coefficients</th>
<th>$r$</th>
<th>RMSE (W m$^{-2}$)</th>
<th>MBE (W m$^{-2}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maykut and Church (1973) [\varepsilon_{cs}=a, \text{where } a=\text{constant}]</td>
<td>$a=0.7248$</td>
<td>0.85</td>
<td>10.9</td>
<td>0.1</td>
</tr>
<tr>
<td>Marshunova (1966) [\varepsilon_{cs}=a+be^{T/2}]</td>
<td>$a=0.5893$ $b=5.351 \times 10^{-3}$</td>
<td>0.88</td>
<td>9.6</td>
<td>0.1</td>
</tr>
<tr>
<td>Swinbank (1963) [\varepsilon_{cs}=aT^b]</td>
<td>$a=9.294 \times 10^{-6}$ $b=2$</td>
<td>0.85</td>
<td>11.9</td>
<td>0.2</td>
</tr>
<tr>
<td>Idso and Jackson (1969) [\varepsilon_{cs}=1-a(e/T)^2]</td>
<td>$a=0.2811$ $b=-3.523 \times 10^{-4}$</td>
<td>0.84</td>
<td>10.8</td>
<td>0.0</td>
</tr>
<tr>
<td>Brutsaert (1973) [\varepsilon_{cs}=a(e/T)^{1/b}]</td>
<td>$a=0.6684$ $b=10$</td>
<td>0.88</td>
<td>9.5</td>
<td>0.3</td>
</tr>
<tr>
<td>Satterlund (1979) [\varepsilon_{cs}=a(1-e^{-e/T(2016)})]</td>
<td>$a=0.7396$</td>
<td>0.86</td>
<td>10.1</td>
<td>0.0</td>
</tr>
<tr>
<td>Konzelmann et al. (1994) [\varepsilon_{cs}=0.23+a(e/T)^{1/b}]</td>
<td>$a=0.4393$ $b=7$</td>
<td>0.88</td>
<td>9.5</td>
<td>−0.2</td>
</tr>
</tbody>
</table>

Table 2. Calculation statistics of hourly $L_\downarrow$ for all-sky conditions computed from Eq. (1) using three effective emissivity, $\varepsilon_{\text{eff}}$, parameterizations and seven different clear-sky emissivity, $\varepsilon_{cs}$, parameterizations (left, with fitted coefficients). Fitted coefficients for $\varepsilon_{\text{eff}}$ parameterizations ($a$, $p$) are found below the parameterizations. Statistics are the same as in Table 1; $\text{Var}$ gives the independent variables ($T$ is temperature [K], $e$ is vapor pressure [Pa]). Correlation coefficients, $r$, are listed once for each $\varepsilon_{cs}$ parameterization as they did not change by more than 0.01 for the three $\varepsilon_{\text{eff}}$ parameterizations.

<table>
<thead>
<tr>
<th>Clear-sky parameterization ($\varepsilon_{cs}$)</th>
<th>$\text{Var}$</th>
<th>$r$</th>
<th>RMSE (W m$^{-2}$)</th>
<th>MBE (W m$^{-2}$)</th>
<th>RMSE (W m$^{-2}$)</th>
<th>MBE (W m$^{-2}$)</th>
<th>RMSE (W m$^{-2}$)</th>
<th>MBE (W m$^{-2}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maykut and Church (1973) [\varepsilon_{cs}=0.7248]</td>
<td>$\varepsilon$</td>
<td>0.87</td>
<td>18.1</td>
<td>−3.1</td>
<td>18.0</td>
<td>−2.3</td>
<td>17.8</td>
<td>−0.2</td>
</tr>
<tr>
<td>Marshunova (1966) [\varepsilon_{cs}=0.5893+5.351 \times 10^{-3} e^{T/2}]</td>
<td>$T$</td>
<td>0.88</td>
<td>17.2</td>
<td>0.5</td>
<td>17.0</td>
<td>0.5</td>
<td>17.4</td>
<td>0.5</td>
</tr>
<tr>
<td>Swinbank (1963) [\varepsilon_{cs}=9.294 \times 10^{-6}T^2]</td>
<td>$T$</td>
<td>0.85</td>
<td>20.0</td>
<td>−4.7</td>
<td>19.2</td>
<td>−3.6</td>
<td>17.8</td>
<td>0.2</td>
</tr>
<tr>
<td>Idso and Jackson (1969) [\varepsilon_{cs}=1-0.2811(e^{-3.523 \times 10^{-4}(273-T)^2})]</td>
<td>$T$</td>
<td>0.87</td>
<td>18.4</td>
<td>−3.8</td>
<td>18.1</td>
<td>−2.9</td>
<td>17.7</td>
<td>0.2</td>
</tr>
<tr>
<td>Brutsaert (1973) [\varepsilon_{cs}=0.6684(e/T)^{1/10}]</td>
<td>$T, e$</td>
<td>0.89</td>
<td>17.1</td>
<td>1.0</td>
<td>17.0</td>
<td>0.9</td>
<td>17.4</td>
<td>0.6</td>
</tr>
<tr>
<td>Satterlund (1979) [\varepsilon_{cs}=0.7396(1-e^{-e/T(2016)})]</td>
<td>$T, e$</td>
<td>0.88</td>
<td>17.5</td>
<td>−2.2</td>
<td>17.5</td>
<td>−1.7</td>
<td>17.6</td>
<td>0.2</td>
</tr>
<tr>
<td>Konzelmann et al. (1994) [\varepsilon_{cs}=0.23+0.4393(e/T)^{1/7}]</td>
<td>$T, e$</td>
<td>0.89</td>
<td>17.0</td>
<td>0.3</td>
<td>16.9</td>
<td>0.3</td>
<td>17.4</td>
<td>0.4</td>
</tr>
</tbody>
</table>

results in a slight positive bias (0 to 1 W m$^{-2}$) whereas those parameterizations only including temperature reveal a larger negative bias of −2 to −5 W m$^{-2}$.

To further examine model performance, model error is related to measured longwave radiation (exemplified in Fig. 2a for one parameterization). Model error tends to be smallest during times of relatively small (clear-sky) and relatively large (overcast) observed radiation. Largest errors are found during partial cloudiness. Model error during partial cloudiness cannot entirely be attributed to shortcomings in the model. Manual sky observations are biased by the observer, and different cloud fractions can be a result of different cloud types (i.e. broken low-level stratiform clouds may give the same fraction as upper-level cirrus). Also, cloud optical depth and cloud phase (liquid, ice or mixed-phase) have significant influence over the efficiency of $L_{\downarrow}$ emission (Curry et al., 1996; Garrett et al., 2002; Iacobellis et al., 2003; Inoue et al., 2006; Tjemström et al., 2008). Additionally, atmospheric optical depth is not constant, largely dependent upon water vapor and other atmospheric gases, aerosols, the surface albedo and perhaps even sub-visible clouds.

Figure 2b shows the bin-averaged error as a function of observed $L_{\downarrow}$ for all seven $\varepsilon_{cs}$ parameterizations applied to $\varepsilon_{\text{eff}}$ from König-Langlo and Augstein (1994). Systematic deviations are evident for all parameterizations. The general trend for all models is an overestimate of $L_{\downarrow}$ when measured values are small and underestimated $L_{\downarrow}$ when $L_{\downarrow}$ is large. The models converge and trend towards an underestimation of $L_{\downarrow}$ between 260 and 300 W m$^{-2}$. Inter-model spread increases for smaller and larger values, although these should be examined cautiously as the number of observations per bin in those ranges is low (Fig. 2b). For observed values larger than ∼310 W m$^{-2}$, the models deviate into two groups, one which has a bias of roughly −5 W m$^{-2}$ (for $L_{\downarrow}$ between ∼310 and 350 W m$^{-2}$) and a second with a larger negative bias of roughly −10 to −15 W m$^{-2}$. The three models with smaller negative bias all contain vapor pressure in the $\varepsilon_{cs}$ parameterizations while (except for one parameterization) the others with larger biases do not, suggesting that a measure of atmospheric moisture increases in importance as cloud fraction, and hence $L_{\downarrow}$ flux, increases.

To assess the potential for coefficient universality, we adopt coefficients of the Konzelmann et al. (1994) parameterizations for $\varepsilon_{cs}$ and $\varepsilon_{\text{eff}}$ fitted to other glacier sites, and compare results to those obtained by fitting coefficients to our data set. We apply the coefficients obtained by Konzelmann et al. (1994) for a site in Greenland, those found by Klok and Oerlemans (2002) for Morteratschgletscher, Switzerland, and two sets of coefficients derived for two different sites on Pasterze, Austria (Greuell et al., 1997), and compute hourly all-sky $L_{\downarrow}$ for the Storglaciären data set. RMSE, MBE and $r$ range from 19 to 20 W m$^{-2}$, −2 to 7 W m$^{-2}$ and 0.85 to 0.87, respectively. Although correlation statistics are broadly within similar ranges as those obtained from parameter fitting to the Storglaciären data set, results indicate that the relationship between measured and calculated $L_{\downarrow}$ is strengthened using fitted coefficients.
### 4.3 Parameterizing cloud fraction

The relationship between hourly cloud fraction and $\tau$ (Eq. 2) is shown in Fig. 3a. In general, $\tau$ increases as cloud fraction decreases, although the spread in $\tau$ for a specific cloud fraction is large. Much of this scatter is attributed to the difficulty in manual cloud observations, variation in cloud optical depth, cloud phase, surface albedo variation, aerosol scattering and absorption of incoming shortwave radiation $S_{\downarrow}$ and variation of atmospheric optical depth. Variance of observed $L_{\downarrow}$ for different cloud levels (high/mid/low, not shown) was found to be relatively small and of the same order of magnitude for the different levels, suggesting the vertical location of cloud base is not the primary source of scatter and uncertainty in using $\tau$.

A nonlinear cloud fraction parameterization of the form

$$n_{\text{param}}(\tau) = \max \left[ a \tau^b + 1; 0 \right]$$

is developed and fit to observations in Fig. 3a, where $n_{\text{param}}$ is parameterized cloud fraction and $a$ and $b$ are coefficients that are fit to the data using a nonlinear, least squares fit. Equation (3) is substituted for observed cloud fraction $n$ in the $\varepsilon_{\text{eff}}$ parameterizations; we choose the $\varepsilon_{\text{eff}}$ parameterization by König-Langlo and Augstein (1994) as example. Coefficients to Eq. (3) and hourly calculation statistics using Eq. (3) are given in Table 3. Correlation coefficients are reduced, RMSE has increased by ~3–4 W m$^{-2}$ but MBE is still within the same range found when observed cloud fraction is used (Table 2). RMSE ranges roughly between 7–8% of the mean observed $L_{\downarrow}$, the increase resulting from an inability of Eq. (3) to represent the observed variability in cloud fraction (Fig. 3). Calculation error as a function of measured $L_{\downarrow}$ for hourly values is shown in Fig. 4a. Systematic $L_{\downarrow}$ error is similar to that observed earlier when actual cloud fraction

![Cloud fraction as a function of the ratio, $\tau$, of measured incoming shortwave radiation and top of atmosphere shortwave radiation for (a) hourly and (b) daily mean data. The lines are fitted non-linear parameterizations for cloud fraction ($n_{\text{param}}$) as a function of $\tau$; the parameterization equation is found in Table 3. $N$ is the number of observations.](Fig_3.png)

**Fig. 3.** Cloud fraction as a function of the ratio, $\tau$, of measured incoming shortwave radiation and top of atmosphere shortwave radiation for (a) hourly and (b) daily mean data. The lines are fitted non-linear parameterizations for cloud fraction ($n_{\text{param}}$) as a function of $\tau$; the parameterization equation is found in Table 3. $N$ is the number of observations.

was used (Fig. 2a), although the absolute magnitude of errors during partial cloudiness tends to be larger.

This approach is also applied to daily mean data from Storglaciären because surface mass balance models often use daily means as input (e.g. Hock et al., 2007). Since cloud observations were not available throughout the night, daily mean cloud fraction was determined only for days ($N$=51) where the observations indicated little to no change in cloud fraction over a 24-h period; the relationship between daily cloud fraction and $\tau$, including the fitted parameterization (Eq. 3) is shown in Fig. 3b. Coefficients and daily calculation statistics are presented in Table 3 showing larger correlation coefficients, reduced RMSE and MBE around zero. RMSE tends to be lowest for the parameterizations that do not have a measure of vapor pressure in the $\varepsilon_{\text{eff}}$ parameterization. The daily error plot (Fig. 4b) is scattered but the error tends to be centered around zero.

The use of $\tau$ to represent cloud fraction poses some complications, especially in glacier environments. Atmospheric transmissivity depends on variables other than cloud fraction, such as cloud and atmospheric optical depth and surface albedo. Fitzpatrick et al. (2004) emphasize the nonlinear relationship between surface albedo and cloud optical depth. When surface albedo is large, the incoming shortwave radiation flux is enhanced by multiple reflections between the surface and the cloud base. Hence, the relationship between $\tau$ and cloud fraction may vary in time as snow cover changes. Microphysical properties of clouds, along with the aerosol distribution, are known to alter cloud effectiveness.
Table 3. Calculation statistics of hourly and daily mean $L_\downarrow$ using the König-Langlo and Augstein (1994) effective emissivity, $\varepsilon_{\text{eff}}$, parameterization, substituting parameterized cloud fraction $n_{\text{param}}$ for actual cloud fraction $n$, and seven different clear-sky emissivity, $\varepsilon_{\text{cs}}$, parameterizations. $T$ is temperature [K], $e$ is vapor pressure [Pa].

<table>
<thead>
<tr>
<th>Clear-sky parameterization ($\varepsilon_{\text{cs}}$)</th>
<th>Hourly Mean Data</th>
<th>Daily Mean Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>König-Langlo and Augstein (1994)</td>
<td>$\varepsilon_{\text{eff}} = a \varepsilon_{\text{cs}} + b n_{\text{param}}$</td>
<td>$\varepsilon_{\text{eff}} = a \varepsilon_{\text{cs}} + b n_{\text{param}}$</td>
</tr>
<tr>
<td>$a = 0.2176$</td>
<td>$b = 1.5$</td>
<td>$a = 0.2176$</td>
</tr>
<tr>
<td>$n_{\text{param}} = -1.873 r^{3.249} + 1$</td>
<td>$n_{\text{param}} = -6.388 r^{5.178} + 1$</td>
<td></td>
</tr>
</tbody>
</table>

in absorbing and emitting radiation, introducing additional uncertainties in using an atmospheric transmissivity index (Curry et al., 1996; Garrett et al., 2002; Iacobellis et al., 2003; Inoue et al., 2006; Tjernström et al., 2008). Another complication arises due to the geographical location of many glaciers. Often surrounded by terrain, during certain hours of the day this causes shading on the $S_\downarrow$ sensor, which if not corrected for, will lead to falsely parameterized cloud fraction. Because we are using $S_\downarrow$ observations, calculations using $\tau$ are limited to daylight hours, but this is often also the case when using manual cloud observations. Also, only melt season data has been analyzed. Higher latitudes in the Northern Hemisphere winter will be influenced by larger solar zenith angles, which may add bias to the relationship between cloud fraction and atmospheric transmissivity. This requires further investigation to assess the applicability of the cloud cover parameterization in other regions. Nevertheless, our results indicate that our simple cloud fraction parameterization performs surprisingly well considering its simple form and the large scatter between $\tau$ and cloud fraction.

4.4 Cloud factor

Rather than including a secondary cloud fraction parameterization within the $\varepsilon_{\text{eff}}$ parameterizations as performed above, we attempt to parameterize cloud factor $F$ as a function of atmospheric transmissivity $\tau$, directly. Figure 5 shows the relationship between $F = L_\downarrow / (\varepsilon_{cs} \sigma T^4)$ and $\tau$ for hourly and daily observations. Scatter between $F$ and $\tau$ is considerable, but in general $F$ increases as $\tau$ decreases. The fitted parameterization equations are provided in the figure. Error plots (Fig. 6a–b) using the cloud factor parameterization (combined with $\varepsilon_{cs}$ parameterization from Konzelmann et al., 1994) are found to be similar to the models using observed cloud fraction (Fig. 2a) and the cloud fraction parameterization above (Fig. 4a–b). Hourly calculations result in $r=0.81$, RMSE=21.8 W m$^{-2}$ and MBE=2.0 W m$^{-2}$. Daily calculations show a strengthening in correlation between calculated and measured values with $r=0.92$, RMSE=14.6 W m$^{-2}$ and MBE=1.8 W m$^{-2}$. These statistics are nearly identical to those obtained when cloud fraction was parameterized using the same atmospheric transmissivity index.

5 Conclusions

With coefficients fitted to the Storglaciären data set, all tested longwave radiation parameterizations differ only slightly in their performance when compared to hourly observations. RMSE for seven tested $\varepsilon_{cs}$ parameterizations range from 10 to 12 W m$^{-2}$ under clear-sky conditions and from 17 to 20 W m$^{-2}$ under all-sky conditions using three $\varepsilon_{eff}$ parameterizations, each combined with the seven $\varepsilon_{cs}$ parameterizations. Clear-sky cases are modelled most accurately.
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